

Cities as Complex Systems II

Individual and Collective Agents, Dynamics, Information

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**Mansueto Institute
for Urban Innovation**

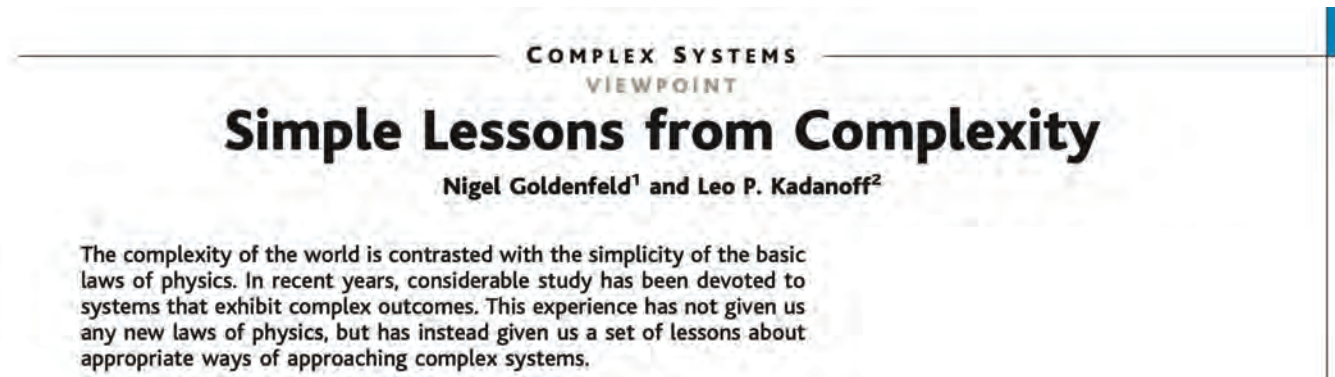


The next few years are likely to lead to an increasing study of complexity in the context of statistical dynamics, with a view to better understanding physical, economic, social, and especially biological systems.

It will be an exciting time.

As science turns to complexity, one must realize that complexity demands attitudes quite different from those heretofore common in physics.

Goldenfeld & Kadanoff, *Science*, 1999



<https://www.science.org/doi/10.1126/science.284.5411.87>



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From statistical physics to social sciences / *De la physique statistique aux sciences sociales*

Towards a statistical mechanics of cities

Vers une mécanique statistique des villes

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Canonical modeling in physics

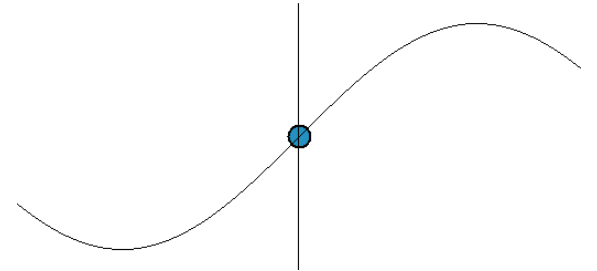
$$\dot{x} = \frac{p}{m}, \quad \dot{p} = -\frac{dV(x)}{dx}$$

position momentum

energy

$$E(x, p) = \frac{p^2}{2m} + V(x)$$

$$\dot{x} \equiv \frac{dx}{dt}$$



Credit : wikipedia

Example: $V(x) = gx^2$

Harmonic oscillator

Conservation of Energy (micro-canonical ensemble)

$$\dot{E} = \frac{p}{m}\dot{p} + \frac{dV(x)}{dx}\dot{x} = -\frac{p}{m}\frac{dV(x)}{dx} + \frac{dV(x)}{dx}\frac{p}{m} = 0.$$

Canonical modeling in physics, in contact with heat reservoir

$$\dot{x} = \frac{p}{m},$$

position

$$\dot{p} = -\gamma p - \frac{dV(x)}{dx} + \chi$$

momentum

random force (thermal)

dissipative force

Internal energy

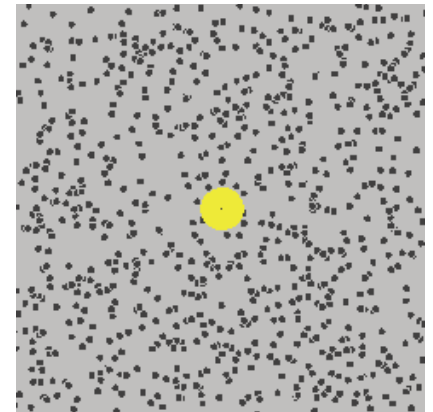
$$E(x, p) = \frac{p^2}{2m} + V(x)$$

Conservation of Energy (canonical ensemble)

$$\dot{E} = \frac{p}{m} \dot{p} + \frac{dV(x)}{dx} \dot{x} = -\frac{p}{m} \left(\gamma p + \frac{dV(x)}{dx} - \chi \right) + \frac{dV(x)}{dx} \frac{p}{m} = -2\gamma \frac{p^2}{2m} + 2\gamma k_B T$$

$$P(p) = \frac{1}{Z} e^{-\frac{p^2}{2mk_B T}}$$

Maxwell-Boltzmann distribution



Credit : wikipedia

$$\rightarrow T_k = \frac{p^2}{2m} = k_B T$$

Thermalization (equipartition in 2D)

Particles in Physics are identical

They are passive: lack 'behavior'

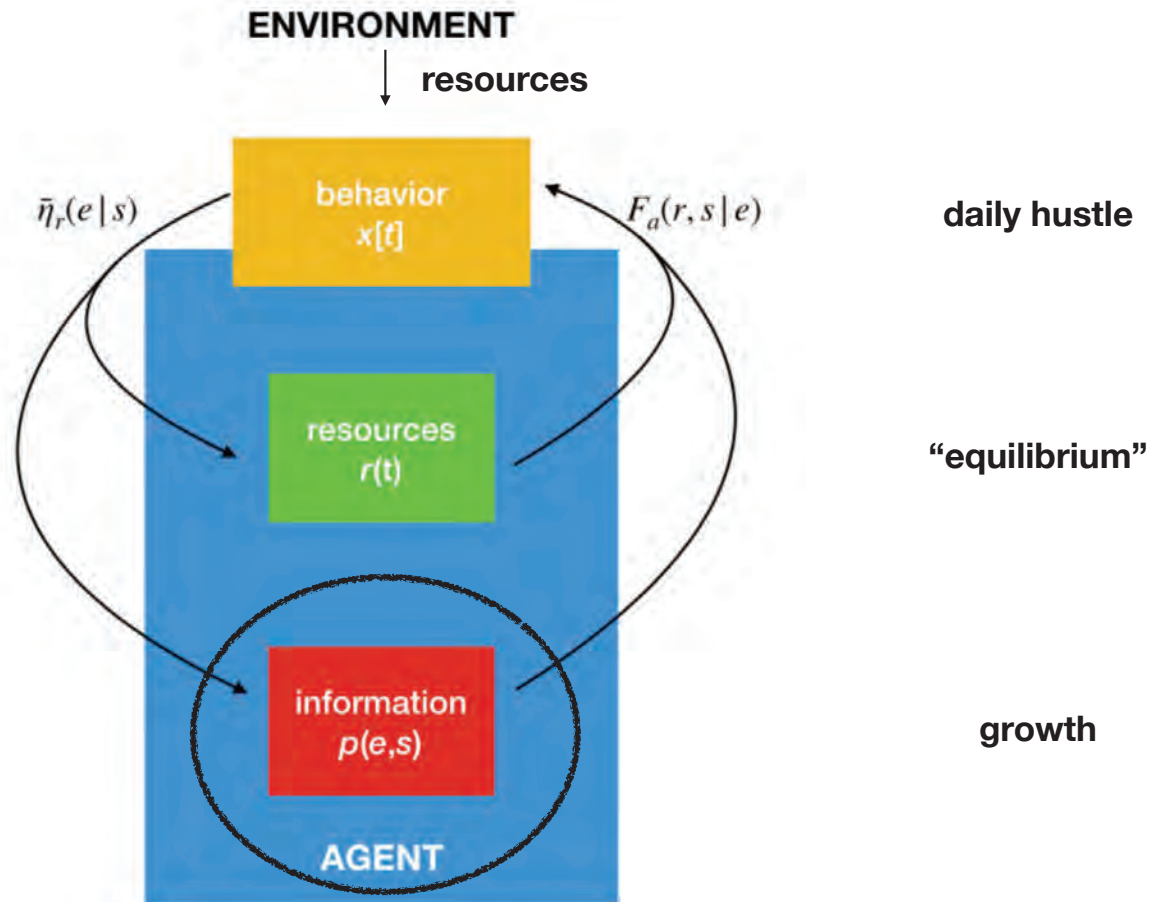
They are purposeless: lack intention

The situation is completely different for agents in complex systems

This requires ability to exert forces that underlie behavior, and make choices between courses of action

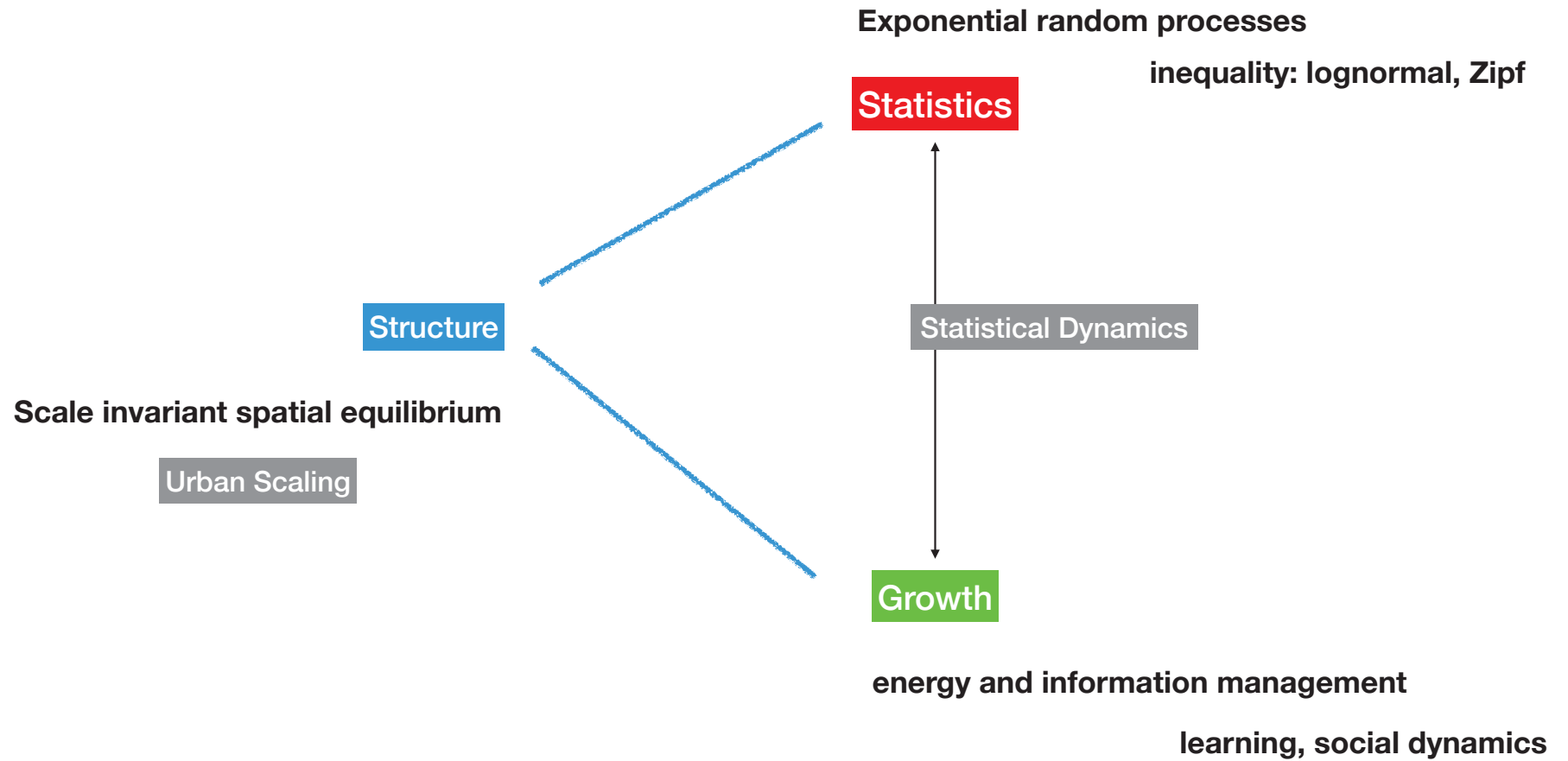
This requires reservoirs of both **energy** and **information**

The general agent in complex systems



Strategic active agents manage resources purposefully in stochastic environments

This has a macroscopic expression for complex systems, such as cities



1. Behavior

$$\dot{x} = p/m, \quad \dot{p} = -\gamma p - \frac{dV(x)}{dx} + \chi + F_a$$

$$[\gamma] = 1/t$$

self-propelled force, selecting position and velocity

Conservation of energy:

$$\Delta E = -2(\gamma \Delta t) \left\langle \frac{p^2}{2m} \right\rangle + 2(\gamma \Delta t) k_B T + \oint F_a \cdot dx$$

Work done by the self-propelling force over a cycle

$$\left\langle \frac{p^2}{2m} \right\rangle = \cancel{k_B T} + \overset{\text{small}}{\frac{1}{2(\gamma \Delta t)}} W_a$$

$$W_a = \oint F_a \cdot dx$$

$$\bar{E} = \left\langle \frac{p^2}{2m} \right\rangle \simeq \frac{1}{2(\gamma \Delta t)} W_a \equiv \bar{w}_a$$

Observed energy is now dominated by behavioral forces

$$P(p_1, p_2) = \frac{1}{Z} e^{-\frac{p_1^2 + p_2^2}{2m\bar{w}_a}}$$

The temperature is the work per unit of dissipation

depends on statistics of \bar{w}_a

2. Energy dynamics

A Model of Resource Dynamics

$$\frac{dr(t)}{dt} = \underbrace{y(t)}_{\text{income}} - \underbrace{c(t)}_{\text{cost}} = \eta_r(t)r(t)$$

“one-good wealth accumulation model”

e.g. Piketty

change in resources

stock: wealth, energy

savings rate = growth rate

growth

“spatial equilibrium”

$$\eta_r(t) \equiv \frac{y(t)}{r(t)} - \frac{c(t)}{r(t)}. \quad \text{definition}$$

Solution:

$$\ln \frac{r(t)}{r(0)} = \left(\bar{\eta}_r - \frac{\sigma_r^2}{2} \right) t + \Theta(t), \quad \text{noise: } \Theta(t) = \sum_{l=1}^t \varepsilon_r(t_l), \quad \longrightarrow \quad \text{Normal}$$

Two independent parameters:

Exponential random processes

$$\gamma = \bar{\eta}_r - \sigma_r^2/2$$

Growth rate

at different scales



Inequality



Objectives:

$$\bar{\eta}_r$$

average growth rate

maximize

learning of relevant information

change through new knowledge

$$\sigma_r$$

“volatility”

minimize

control: households, government

stability, resilience



The counter intuitive consequences of stochastic geometric growth

Consequences:

zero average, standard deviation: $\sigma_{\Theta} = \sigma_r \sqrt{t}$

$$1. \quad \ln \frac{r(t)}{r(0)} = \left(\bar{\eta}_r - \frac{\sigma_r^2}{2} \right) t + \Theta(t),$$

$$= \gamma_r$$

$$\Theta(t) = \sum_{l=1}^t \varepsilon_r(t_l) \sim \sigma_r \sqrt{t}$$

Central Limit Theorem -> Gaussian

lognormal statistics !!

$$2. \quad \frac{1}{t} \ln \frac{r(t)}{r(0)} = \gamma_r + \frac{\Theta(t)}{t} \rightarrow \gamma_r,$$

The average growth rate over long times becomes a simple number

ergodicity (population dynamics)

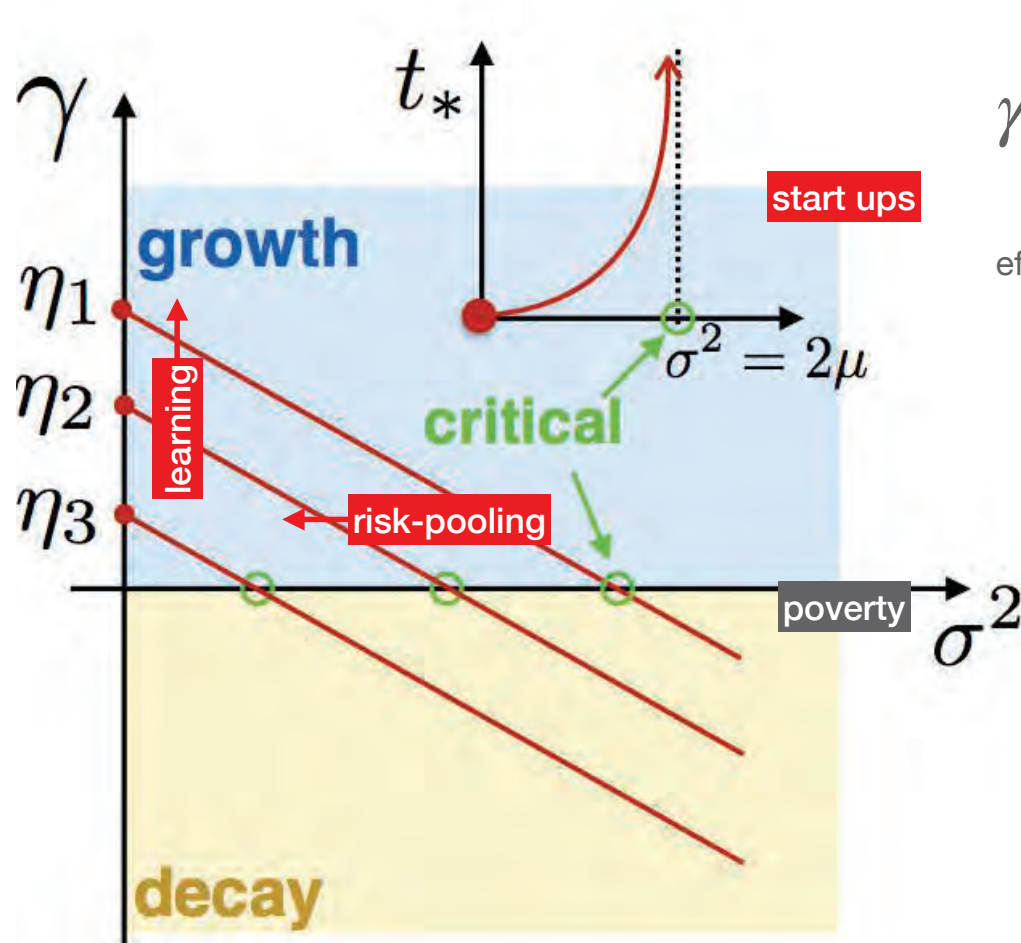
$$3. \quad t_* = \frac{\sigma_r^2}{\left(\bar{\eta}_r - \frac{\sigma_r^2}{2} \right)^2},$$

There is a minimum time to see through the “fog” of sort term fluctuations.

proportional to the uncertainty (volatility, std) between relative income and costs

people with a lot of uncertainty do not see growth as a possibility

Phase diagram



$$\gamma = \eta - \frac{\sigma^2}{2}$$

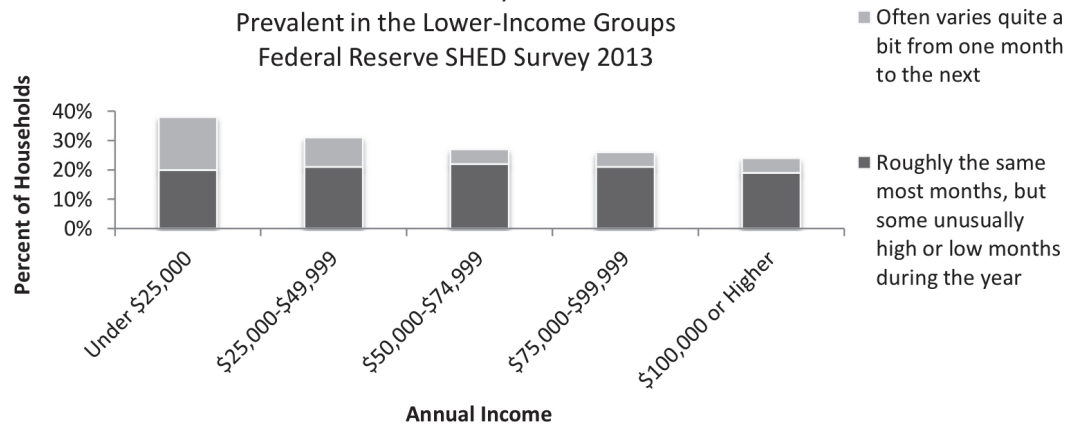
effective growth rate

Net Growth Requires Low Fluctuations

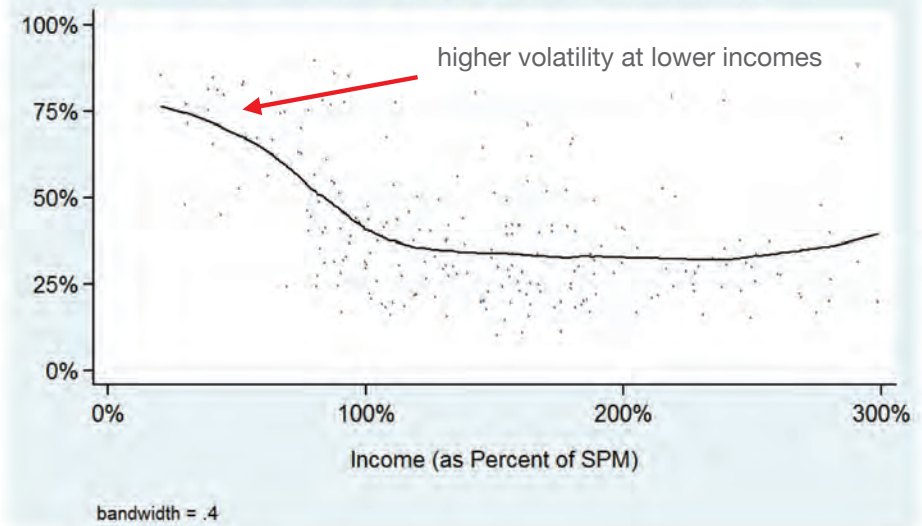
Poverty is a low resources, high volatility state

lower effective growth rates, unclear horizons

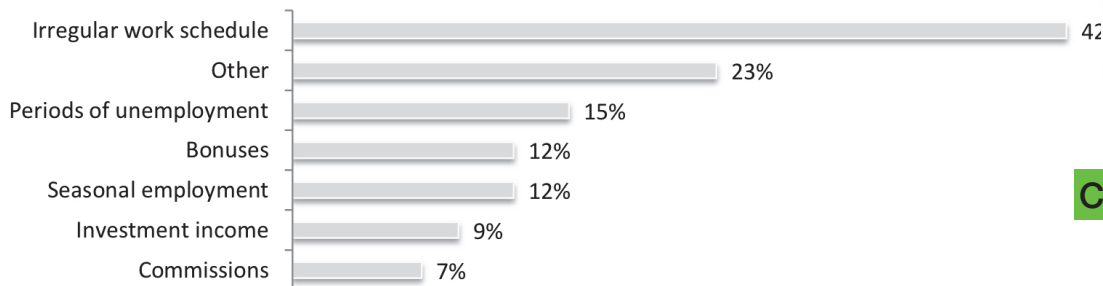
Income Variability is More Prevalent in the Lower-Income Groups
Federal Reserve SHED Survey 2013



Lowess of Volatility (CV) of Monthly Household Income on Income Level (as Percent of SPM)



Why does your income change from month to month?
Federal Reserve SHED Survey 2013



Can this be studied using registry data in the Netherlands?

from: Income Gains and Month-to-Month Income Volatility: Household evidence from the US Financial Diaries: Hannagan + Morduch (2015)

How to lower volatility? How to derive lognormal and power law statistics?



SCIENCE ADVANCES | RESEARCH ARTICLE

SOCIAL SCIENCES

Urban growth and the emergent statistics of cities

Luis M. A. Bettencourt^{1,2}

Urban theory models cities as spatial equilibria to derive their aggregate properties as functions of extensive variables, such as population size. However, this assumption seems at odds with cities' most interesting properties as engines of fast and variable processes of growth and change. Here, we build a general statistical dynamics of cities across scales, from single agents to entire urban systems. We include agents' strategic behavior to produce predictable growth rates, which requires balancing relative incomes and costs over time. We implement these dynamics using stochastic differential equations and control theory to demonstrate a number of general emergent properties of cities deriving from limit theorems applied to growth rates. This framework establishes necessary conditions for scaling to be conserved by urban dynamics and shows how exponent corrections can be calculated. These ideas are tested using stochastic simulations and a long timeseries for 382 US Metropolitan Areas over nearly five decades.

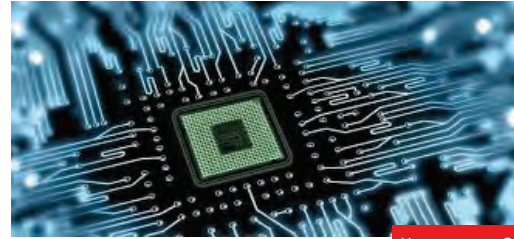
<https://www.science.org/doi/epdf/10.1126/sciadv.aat8812>

Feedback Control is a big part of your life





“stable” airplanes



“error free” computers



Self-driving cars



Balancing humans and robots

Want low fluctuations:

$$\eta_r(t) \equiv \frac{y(t)}{r(t)} - \frac{c(t)}{r(t)} = b(t) - a(t) = \bar{\eta} + u(t) - v(t) = \bar{\eta} + \epsilon(t)$$

definition

income fluctuations

choice expenditures

definition

The diagram shows the equation $\eta_r(t) \equiv \frac{y(t)}{r(t)} - \frac{c(t)}{r(t)} = b(t) - a(t) = \bar{\eta} + u(t) - v(t) = \bar{\eta} + \epsilon(t)$. A red curved arrow labeled 'definition' points from the first two terms to the third. A black arrow labeled 'income fluctuations' points from $u(t)$ to the text 'income fluctuations'. A black arrow labeled 'choice expenditures' points from $v(t)$ to the text 'choice expenditures'. Another red curved arrow labeled 'definition' points from the last two terms to the first.

when I have more money can spend more and vice-versa

Consumption Smoothing

need to average (smoothen) expenditures and incomes over some time
month, season, year

How Control theory works:

PID Controller

$$u(t) = k_P \varepsilon_r(t) + k_I \int_0^t \varepsilon_r(t') dt' + k_D \frac{d\varepsilon_r}{dt}, \quad \text{Time costs to track income fluctuations}$$

This gives a simple dynamics for errors

$$\cancel{\frac{d^2 \varepsilon_r}{dt^2}} + 2\zeta \omega \frac{d\varepsilon_r}{dt} + \omega^2 \varepsilon_r = F/m, \quad m = k_D, \omega = \sqrt{k_I/k_D} \text{ and } \zeta = \frac{k_P+1}{2\sqrt{k_D k_I}},$$

noisy spring

$$d\varepsilon_r = -\frac{M}{2} \varepsilon dt + \Omega dW(t).$$

error wants to vanish

noise

$$M = \omega/\zeta = k_I/[2(k_P + 1)]$$

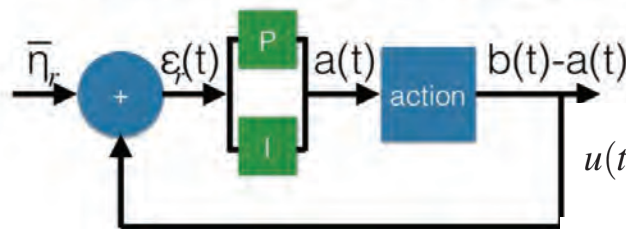
Statistics of error is “under control”:

$$P[\varepsilon_r, t | \varepsilon_0] = \sqrt{\frac{M}{2\pi\Omega^2(1 - e^{-Mt})}} e^{-\frac{M}{2\Omega^2} \left[\frac{(\varepsilon_r - \varepsilon_0 e^{-M/2 t})^2}{1 - e^{-Mt}} \right]} \rightarrow \sqrt{\frac{M}{2\pi\Omega^2}} e^{-\frac{M}{2\Omega^2} \varepsilon_r^2},$$

quality of control

Why are relative incomes and costs correlated?

Control Scheme for Savings and Growth



“Consumption Smoothing”

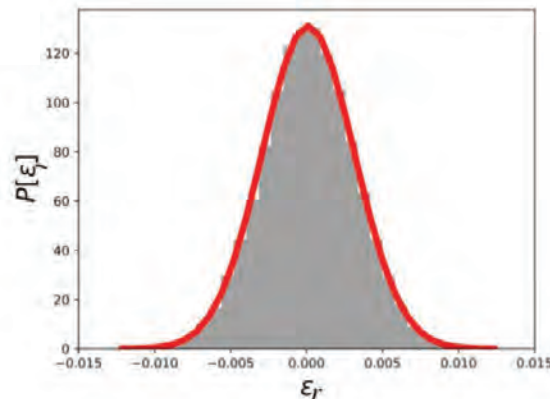
$$u(t) = k_P \epsilon_r(t) + k_I \int_0^t \epsilon_r(t') dt' + k_D \frac{d\epsilon_r}{dt},$$

$$k_D \frac{d^2 \epsilon_r}{dt^2} + (k_P + 1) \frac{d\epsilon_r}{dt} + k_I \epsilon_r = \frac{dv}{dt}.$$

damped harmonic oscillator + noise

$$\sigma_\epsilon^2 = 2\Omega^2 \frac{k_P + 1}{k_I}$$

controlled by time-averaging of error



growth rates become Gaussian & growth is geometric and random

At **larger (population) scales**, there are many more mechanisms:

- insurance
- pension funds
- government social services
- corporate 'bail-outs'

How to increase growth rates?

Editors' Pick for #1 Nonfiction Book of 2005 —Amazon.com

Fortune's Formula



THE UNTOLD STORY

OF THE SCIENTIFIC BETTING SYSTEM THAT BEAT

THE CASINOS AND WALL STREET

William Poundstone

1st
2nd 12
3rd 12
to 1 2 to 1 2 to 1

"Seldom have true crime and smart math been blended together so engagingly."
—Jim Holt, *The Wall Street Journal*

"Fortune's Formula may be the world's first history book, gambling primer, mathematics text, economics manual, personal finance guide and joke book in a single volume. Poundstone comes across like the best college professor you ever had, someone who can turn almost any technical topic into an entertaining and zesty lecture."
—David Pogue, *The New York Times Book Review*

"An amazing story that gives a big idea the needed star treatment . . . Fortune's Formula will appeal to readers of such books as Peter H. Bernstein's *Against the Gods*, Nassim Nicholas Taleb's *Foiled by Randomness*, and Roger Lowenstein's *When Genius Failed*. All try to explain why smart people take stupid risks. Poundstone goes them one better by showing how hedge fund long-term Capital Management, for one, could have avoided disaster by following the Kelly method."

—Peter Coy, *BusinessWeek* (four stars)

William Poundstone is the bestselling author of nine nonfiction books, two of which (*Labyrinths of Reason* and *The Recursive Universe*) were nominated for the Pulitzer Prize.

U.S.A. \$15.00 / Can. \$18.95

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Cover art: Casino roulette keyhole © Red Stone Photoart; Archetype casino chips © Sideshow Gaming Company

Bill and Wang

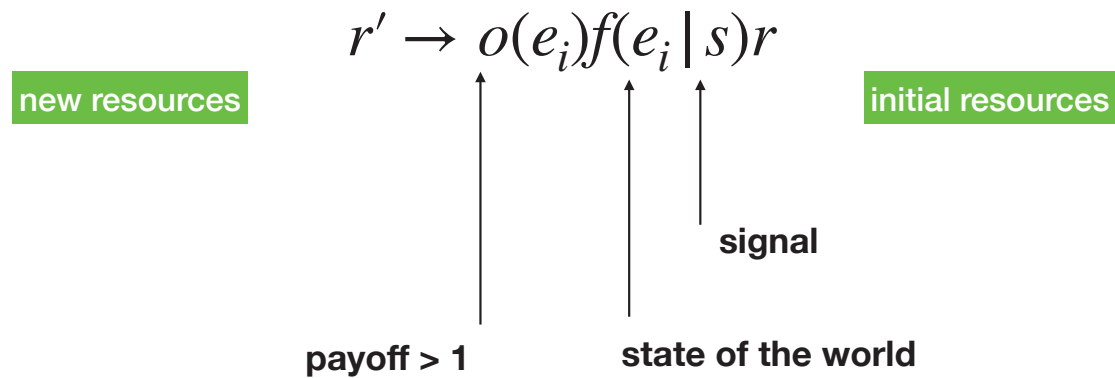
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www.doubleday.com

3. Information

Investment and information

Inter temporal optimization: sequential investment in stochastic environmental outcome



after T steps:

$$r(T) = \prod_{t=1}^T o(e_t)f(e_t | s_t)r(0)$$

average growth rate:

$$\bar{\eta}_r = \lim_{T \rightarrow \infty} \frac{1}{T} \ln \frac{r(T)}{r(0)} = v_T \sum_i P(e_i, s_i) \ln f(e_i | s) o(e_i)$$

Maximal Growth Rate:

Simple intertemporal optimization without discounting

$$\bar{\eta}_r = \lim_{T \rightarrow \infty} \frac{1}{T} \ln \frac{r(T)}{r(0)} = v_T \sum_{e,s} P(e,s) \ln f(e|s) o(e)$$

best allocation: $f(e|s) \rightarrow P(e|s)$

fair odds: $o(e) \rightarrow 1/P(e)$ (worst case = “efficient markets”)

$$\bar{\eta}_r^* = v_T \sum_{e,s} P(e,s) \ln \frac{P(e,s)}{P(e)P(s)} = v_T I[E; S]$$

Shannon's Mutual Information

This is also the **Optimal Predictor of Environment** |_{signal} ~ Bayes ~ Machine Learning
~maximal fitness

Ultimately, this involves developing a new theory of optimal choice:

better than 'rational choice theory', beyond behavioral economics

- intertemporal (life course)
- deals with uncertainty
- social networks, power, distribution: organizations
- consistent across scales



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Current Opinion in Psychology
Volume 33, June 2020, Pages 183-188

The effects of low socioeconomic status on decision-making processes

Jennifer Sheehy-Skeffington

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<https://doi.org/10.1016/j.copsy.2019.07.043> Get rights and content

Highlights

- Low income groups are criticised for making suboptimal decisions in domains such as health and finance.
- These reflect a psychological shift in response to socioecological cues prevalent in low socioeconomic status (SES) contexts.
- Low SES experiences present the cues of resource scarcity, environmental instability, and low subjective social status.
- These trigger a regulatory shift toward present (over future) goals and the up/down-regulation of specific cognitive skills.

<https://www.sciencedirect.com/science/article/pii/S2352250X1930123X?via=ihub>

Population dynamics of growth and learning



 Free Access

The Rules of Information Aggregation and Emergence of Collective Intelligent Behavior

Luís M. A. Bettencourt

First published: 12 October 2009 | <https://doi.org/10.1111/j.1756-8765.2009.01047.x> | Citations: 20

✉ should be sent to Luís M. A. Bettencourt, Theoretical Division, MS B284, Los Alamos National Laboratory, Los Alamos NM 87545; or Luís M.A. Bettencourt, Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, NM 87501. E-mail: imbett@lanl.gov

 SECTIONS



PDF



TOOLS



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Abstract

Information is a peculiar quantity. Unlike matter and energy, which are conserved by the laws of physics, the aggregation of knowledge from many sources can in fact produce more information (synergy) or less (redundancy) than the sum of its parts. This feature



Statistical dynamics of wealth inequality in stochastic models of growth

Jordan T. Kemp ^a, Luis M.A. Bettencourt ^{b, c, d}

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<https://doi.org/10.1016/j.physa.2022.128180>

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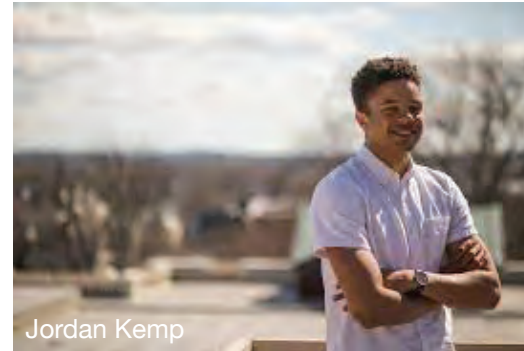
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Highlights

- Agent growth rates and initial resources correlations affect aggregate growth rates.
- Negative correlated growth rate assignments reduce aggregate growth.
- Volatility and growth rate, resource covariance dominate intermediate time dynamics.
- Variances in growth rates across the population dominate long time inequality.
- The effects of heterogeneity on inequality outpace effects on growth.

<https://www.sciencedirect.com/science/article/pii/S0378437122007385>



Jordan Kemp



Volume 2, Issue 4
April 2023

Article Contents

- Abstract
- Introduction
- Theory and modeling of information-based growth
- Population effects of information dynamics

Learning increases growth and reduces inequality in shared noisy environments

Jordan T Kemp, Luis M A Bettencourt Author Notes

PNAS Nexus, Volume 2, Issue 4, April 2023, pgad093,

<https://doi.org/10.1093/pnasnexus/pgad093>

Published: 22 March 2023 Article history

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Abstract

Stochastic multiplicative dynamics characterize many complex natural phenomena such as selection and mutation in evolving populations, and the generation and distribution of wealth within social systems. Population heterogeneity in stochastic growth rates has been shown to be the critical driver of wealth inequality over long time scales. However, we still lack a general statistical theory that systematically explains the origins of these heterogeneities resulting from the dynamical adaptation of agents to their

<https://academic.oup.com/pnasnexus/article/2/4/pgad093/7083303>

Growth rates for individuals vs collectives

Is the growth rate for a city the average of the growth rates for individuals?

Not in general:

$$r_G = \frac{1}{G} \sum_{j=1}^G r_j$$

average wealth

$$\frac{dr_G}{dt} = y_G - c_G = (\eta r)_G,$$

growth of wealth per capita in a population

average of product


$$(\eta r)_G = \frac{1}{G} \sum_{j=1}^G \eta_j w_j = \eta_G r_G + \text{covar}_G(\eta, r) = [\eta_G + \text{covar}_G(\eta, r/r_G)] r_G.$$

average rate

“selection”

Consequences:

$$(\eta r)_G = \frac{1}{G} \sum_{j=1}^G \eta_j w_j = \eta_G r_G + \text{covar}_G(\eta, r) = [\eta_G + \text{covar}_G(\eta, r/r_G)] r_G.$$

average corrected by co-variance 

positive: richer people get higher growth rates
correlation between resources and rates

negative: richer people get lower growth rates
anti-correlation between resources and rates

What situation gives the highest overall growth rates?

What situation gives the lowest inequality?

This is an instance of a very general result

Price Equation of Selection:

$$\bar{\gamma} \Delta \bar{z} = \text{covar}(z, \gamma) + E[\gamma \Delta z]$$

average growth rate average trait change

Pure selection

$$z = \gamma$$

$$\Delta \bar{\gamma} = \frac{\sigma_{\gamma}^2}{\bar{\gamma}} \geq 0.$$

Fisher's Fundamental Theorem

Selection in a heterogeneous population creates growth
Monopoly arrests growth increases to the dominant type

Increasing growth in a population or maintaining it under obsolence
requires maintaining population diversity

This is a large-scale, long term result

For N agents we get:

$$I(e; \{s_i\}) = H[e] - H[e|\{s_i\}]$$
$$= - \sum_{i=1}^N \frac{\Delta H[e]}{\Delta s_i} - \sum_{i>j=1}^N \frac{\Delta^2 H[e]}{\Delta s_i \Delta s_j} - \dots - \frac{\Delta^N H[e]}{\Delta s_1 \dots \Delta s_N},$$
$$-\frac{\Delta H[e]}{\Delta s_i} = H[e] - H[e|s_i] = I(e, s_i);$$

For 2 agents we get:

$$I(e; \{s_1, s_2\}) = I(e; s_1) + I(e; s_2) - R_I(e; s_1, s_2); \quad R_I(e; s_1, s_2) = I(s_1; s_2) - I(s_1; s_2|e)$$

Coefficient of redundancy

Coordination given environment

Properties of Information and Institutions

Many problems need organizations: firms, NGOs, governments

Information in a group

$$I(E; \{S_1, S_2, \dots, S_N\}) \begin{matrix} < \\ = \\ > \end{matrix} \sum_{i=1}^N I(E; S_i) \begin{matrix} \text{redundancy} \\ \text{independence} \\ \text{synergy} \end{matrix}$$

more than the sum of the parts

The advantage of collective action requires synergy : diverse collective institutions

to evaluate quality of an institution (group)

compare individual action to collective production

$$\Delta r_i = I(E; S_1)r_i(0) - c_i$$

Individual knowledge

$$\Delta r_i = B_i I(E; \{S_1, S_2, \dots, S_N\})r_i(0) - C_i$$

distribution
of collective gains

collective knowledge

collective costs

Collaborating in the groups is preferred when:

$$B_i I(E; \{S_1, S_2, \dots, S_N\}) > I(E; S_i) + \frac{C_i - c_i}{r_i(0)}$$

'fair' re-distribution of gains

↑
strong synergy

↑
low individual information

low costs of collective action vs individual cost

cities / firms are good at strong synergies, lower collective costs; but not always fair distribution

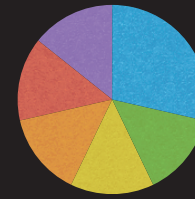
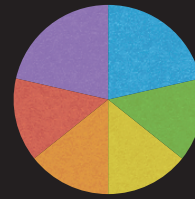


Poor

autarky (subsistence)

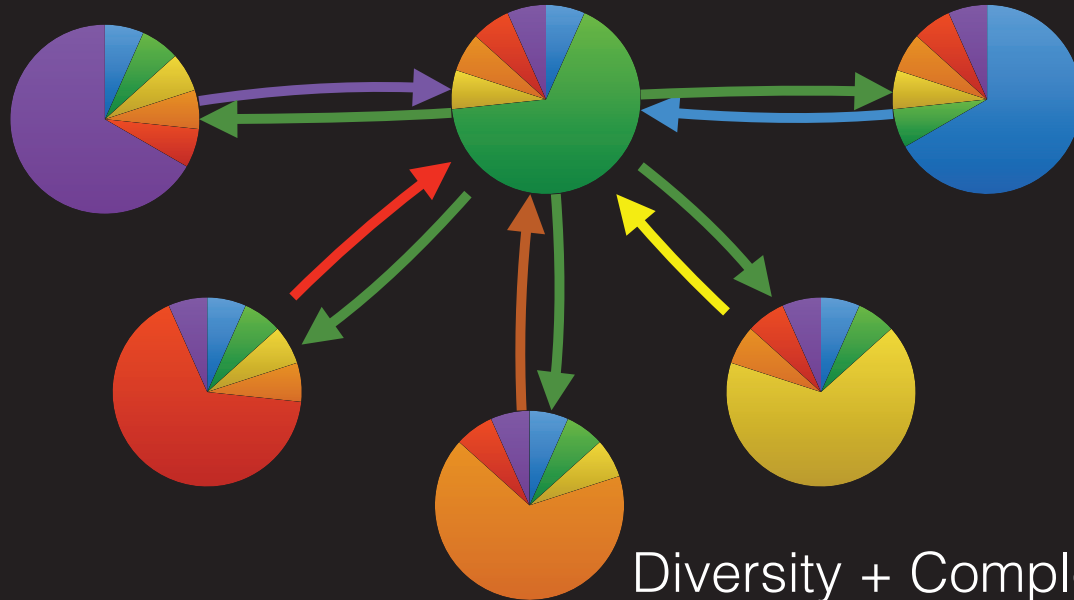


Redundancy



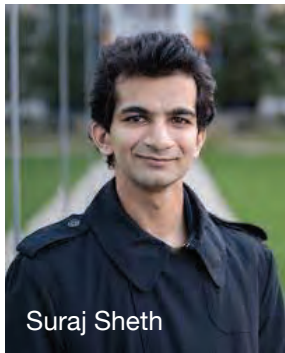
Rich

cosmopolitanism



Human development as a network process (in cities)

1. Measuring Human Development across scales



[nature](#) > [npj urban sustainability](#) > [articles](#) > [article](#)

Article | [Open Access](#) | [Published: 20 February 2023](#)

Measuring health and human development in cities and neighborhoods in the United States

[Suraj K. Sheth](#)  & [Luis M. A. Bettencourt](#)

[npj Urban Sustainability](#) **3**, Article number: 7 (2023) | [Cite this article](#)

<https://www.nature.com/articles/s42949-023-00088-y>

Procedural Inequality:

Equality of What?

AMARTYA SEN

THE TANNER LECTURE ON HUMAN VALUES

Delivered at
Stanford University

May 22, 1979

“capabilities approach”

https://www.ophi.org.uk/wp-content/uploads/Sen-1979_Equality-of-What.pdf

Critique of

1. Marginal Utility
2. Total Utility (welfarism)
3. Rawls Liberalism

basic capabilities

agency

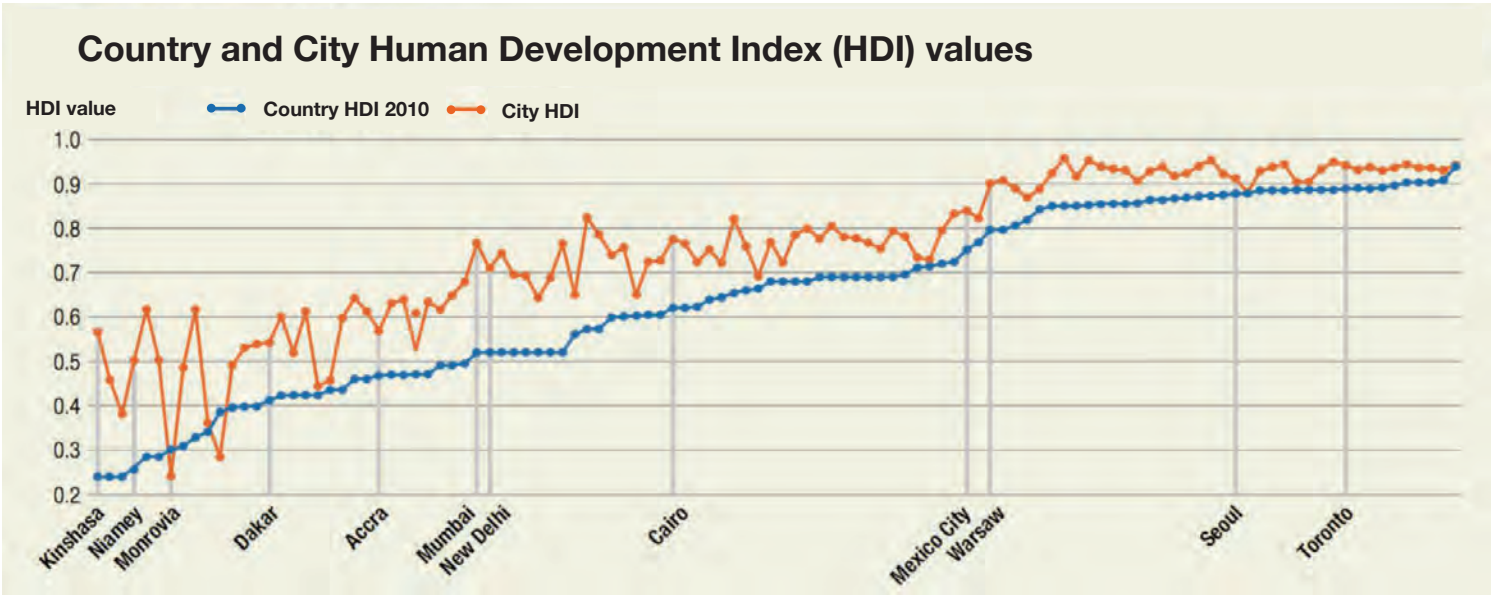
empowerment

not money, goods, freedom,...

+ Martha Nussbaum

<https://ir.lawnet.fordham.edu/cgi/viewcontent.cgi?article=3391&context=fir>

Broad Human Development is a Feature of Larger Cities !



credit: UNDP Human Development Report 2013

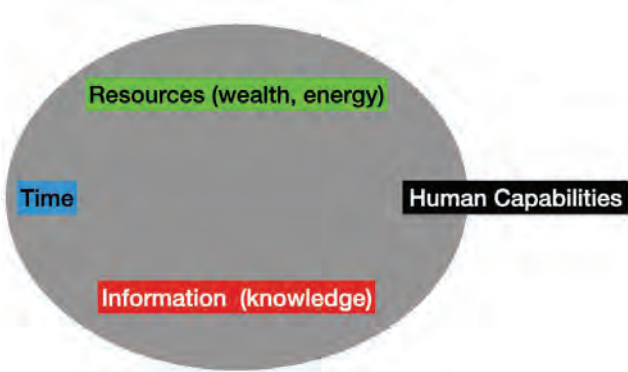
Human Development Index

“measures the ability of human populations to lead, long, healthy and fulfilled lives”



Mahbub ul Haq

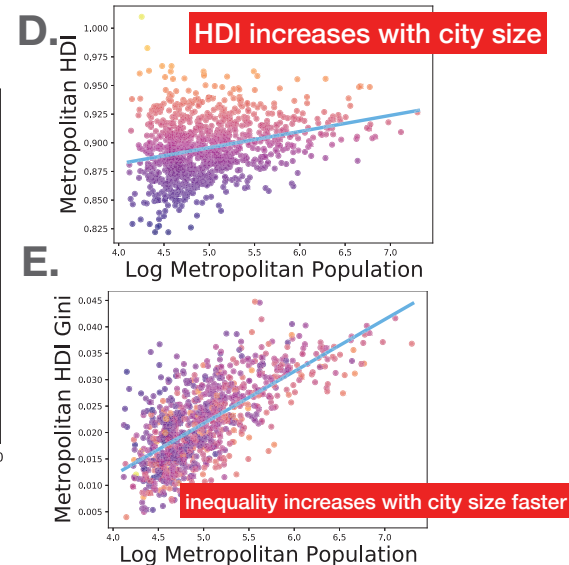
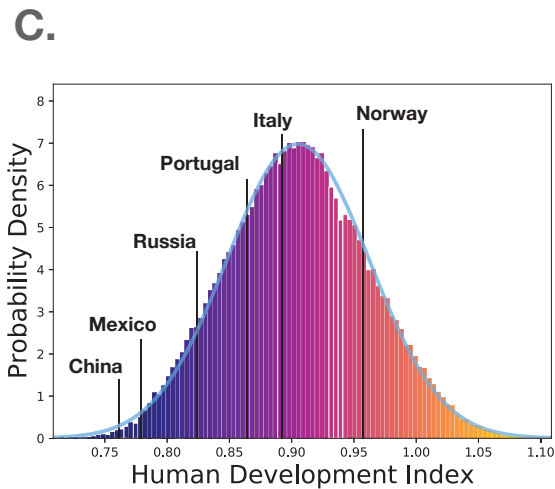
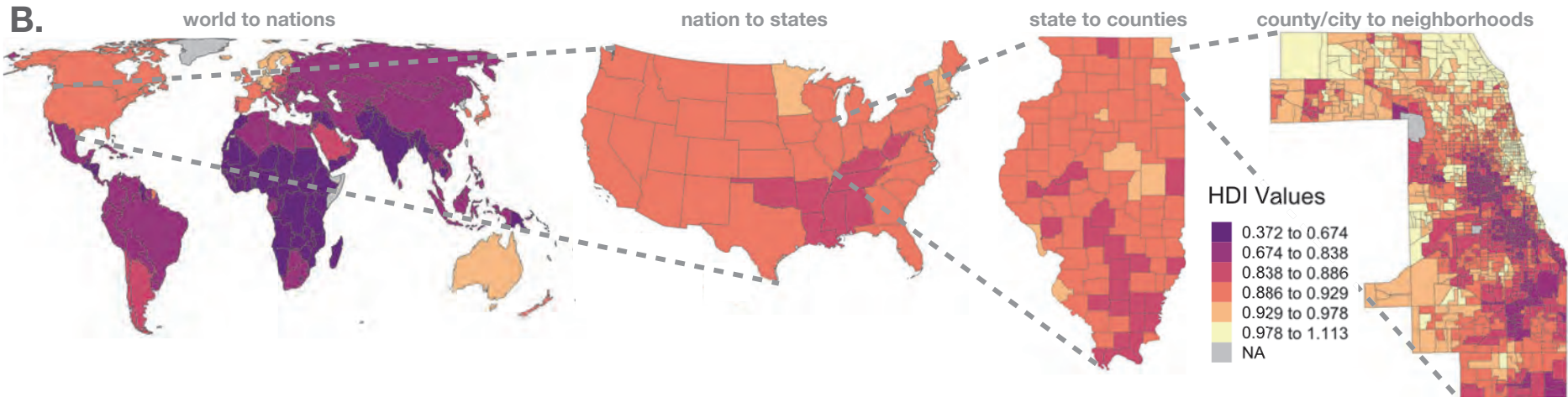
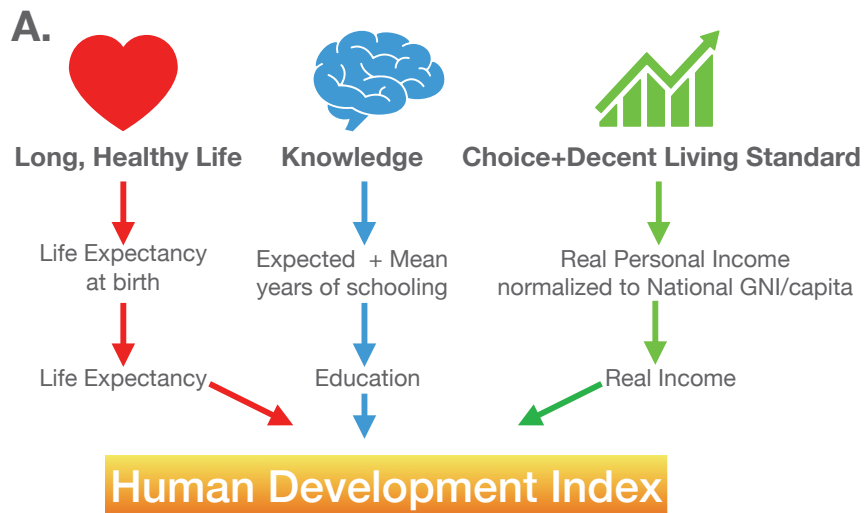
$$HDI_i = \left(education_i \cdot life\ expectancy_i \cdot real\ income_i \right)^{1/3}$$



The US is now # 17

because of health and educational inequality

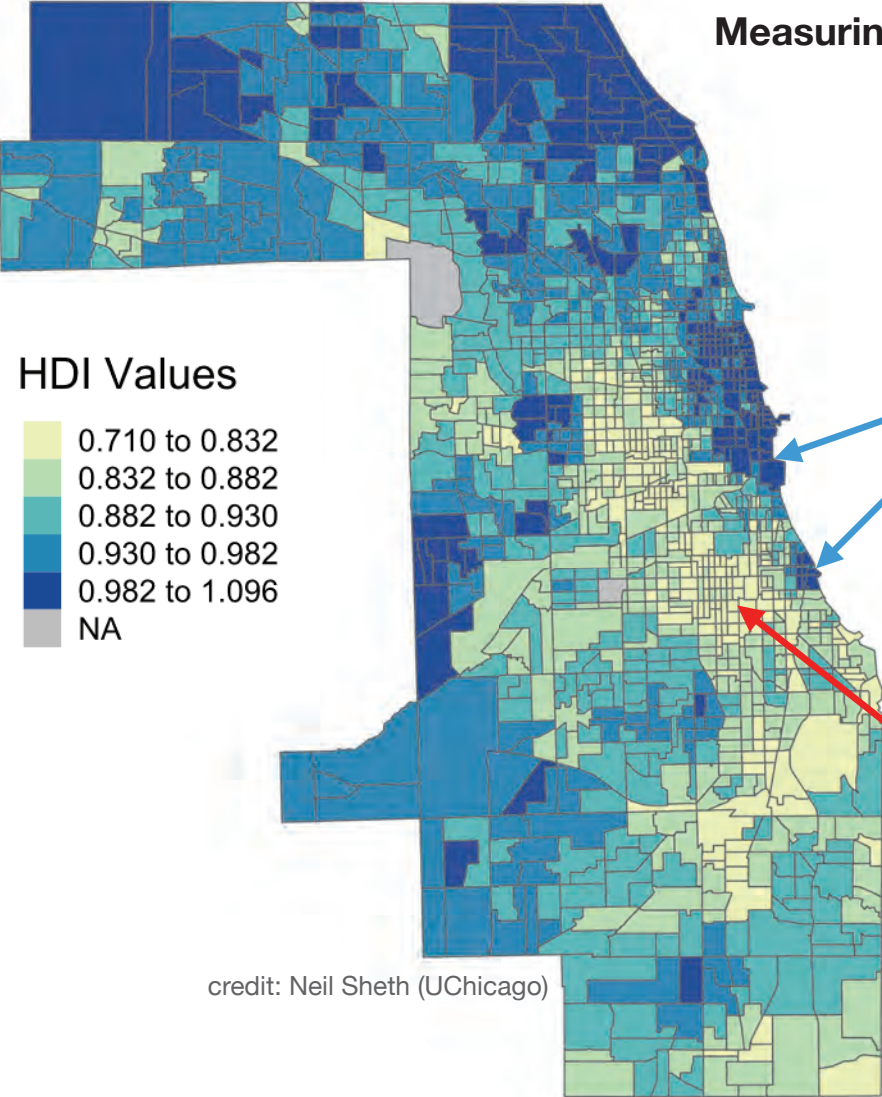
Rank		Country or Territory	HDI	
2019 data (2020 report) ^[14]	Change over 5 years (2014) ^[15]		2019 data (2020 report) ^[14]	Average annual HDI growth (2010-2019) ^[15]
1	—	Norway	0.957	▲ 0.20%
2	▲ (7)	Ireland	0.955	▲ 0.65%
2	—	Switzerland	0.955	▲ 0.16%
4	▲ (7)	Hong Kong	0.949	▲ 0.54%
4	▲ (4)	Iceland	0.949	▲ 0.62%
6	▼ (3)	Germany	0.947	▲ 0.24%
7	▼ (3)	Sweden	0.945	▲ 0.41%
8	▼ (2)	Australia	0.944	▲ 0.17%
8	▼ (1)	Netherlands	0.944	▲ 0.32%
10	▼ (6)	Denmark	0.940	▲ 0.28%
11	▼ (2)	Finland	0.938	▲ 0.26%
11	—	Singapore	0.938	▲ 0.35%
13	—	United Kingdom	0.932	▲ 0.24%
14	▲ (1)	Belgium	0.931	▲ 0.25%
14	▲ (3)	New Zealand	0.931	▲ 0.30%
16	▼ (1)	Canada	0.929	▲ 0.34%
17	▼ (3)	United States	0.926	▲ 0.12%



https://papers.ssrn.com/sol3/papers.cfm?abstract_id=3961750

Check out the interactive map at: <https://communityhdi.org/>

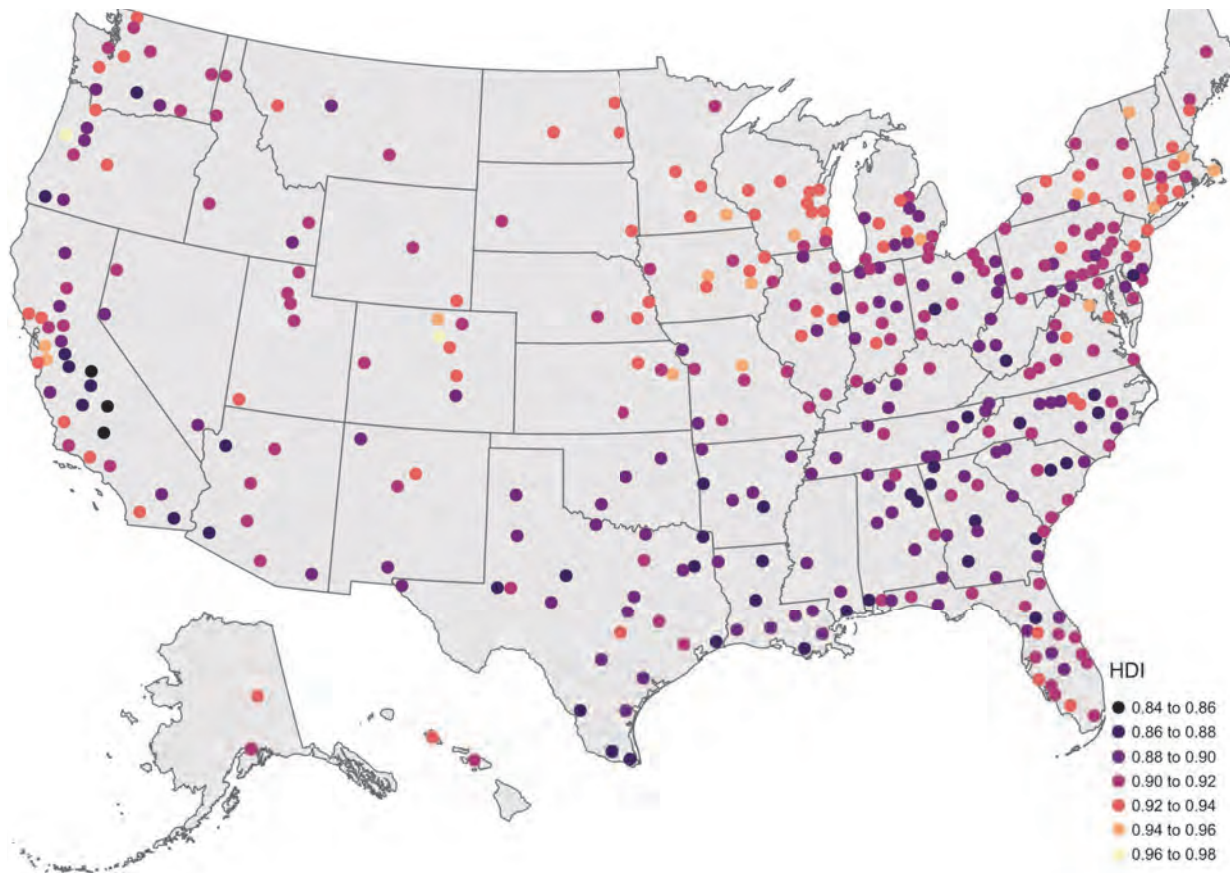
Measuring the Human Development of Chicago neighborhoods



better than Norway

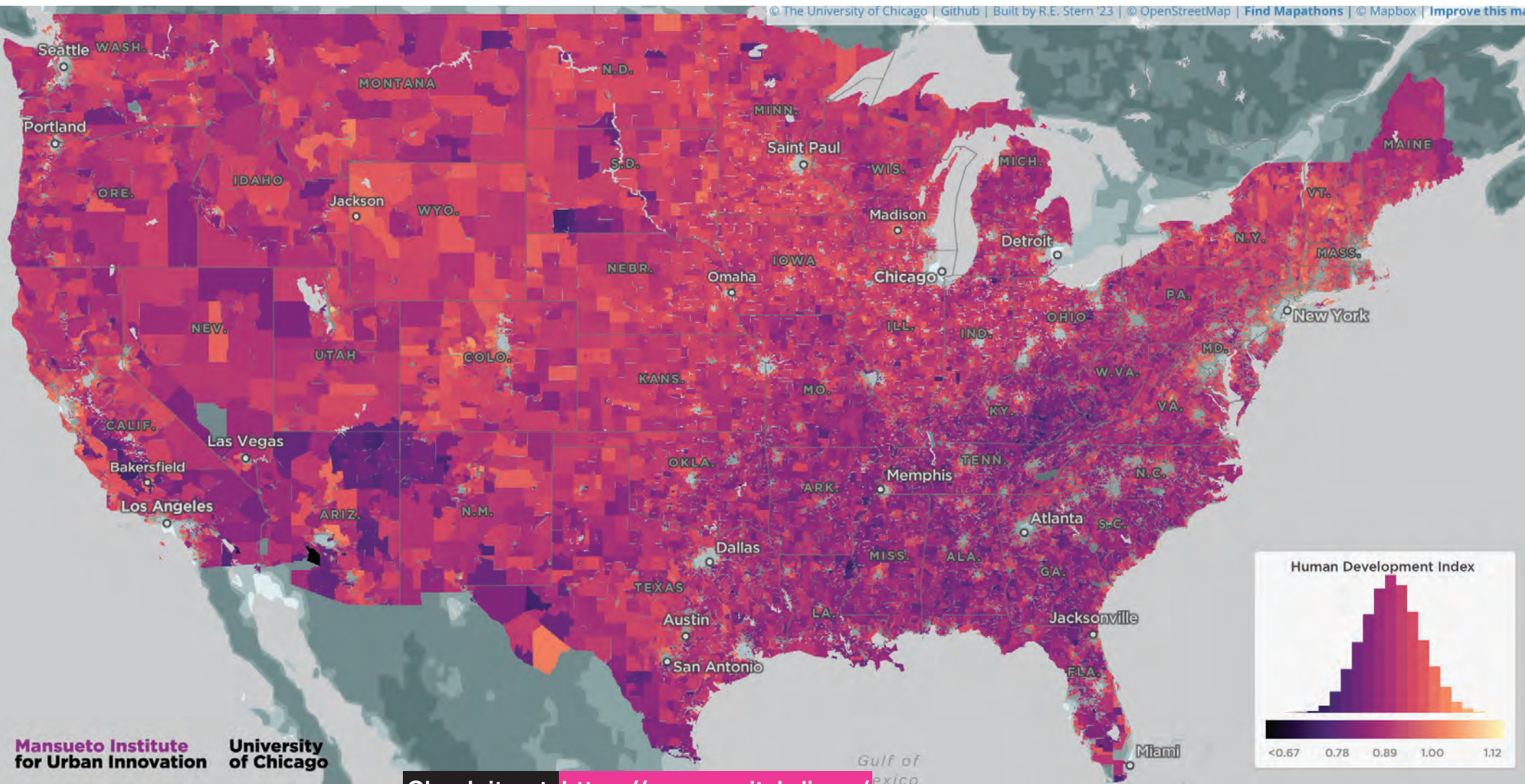
worse than China or Mexico

credit: Neil Sheth (UChicago)



State/Federal District	HDI	Metropolitan Area	HDI
Massachusetts	0.9407	Boulder, CO	0.9624
Connecticut	0.9378	Corvallis, OR	0.9622
Vermont	0.9348	Ann Arbor, MI	0.9570
New Hampshire	0.9345	Iowa City, IA	0.9567
Minnesota	0.9330	San Jose-Sunnyvale-Santa Clara, CA	0.9557
New Jersey	0.9281	Bridgeport-Stamford-Norwalk, CT	0.9553
District of Columbia	0.9273	Ames, IA	0.9532
Maryland	0.9271	Lawrence, KS	0.9496
North Dakota	0.9244	Boston-Cambridge-Newton, MA-NH	0.9491
Colorado	0.9240	San Francisco-Oakland-Hayward, CA	0.9486
Texas	0.8964	Gadsden, AL	0.8647
South Carolina	0.8935	McAllen-Edinburg-Mission, TX	0.8641
Nevada	0.8919	Lake Havasu City-Kingman, AZ	0.8637
Oklahoma	0.8879	Laredo, TX	0.8614
Tennessee	0.8874	Dalton, GA	0.8614
Kentucky	0.8843	Brownsville-Harlingen, TX	0.8605
Alabama	0.8839	Yakima, WA	0.8604
Louisiana	0.8838	Pine Bluff, AR	0.8601
West Virginia	0.8832	Bakersfield, CA	0.8595
Arkansas	0.8798	Visalia-Porterville, CA	0.8579
Mississippi	0.8762	Madera, CA	0.8572

https://papers.ssrn.com/sol3/papers.cfm?abstract_id=3961750



Mansueto Institute for Urban Innovation University of Chicago

Check it out: <https://communityhdi.org/>

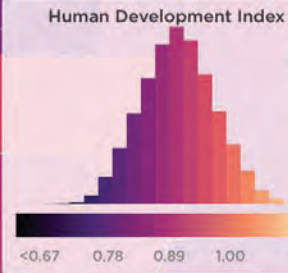
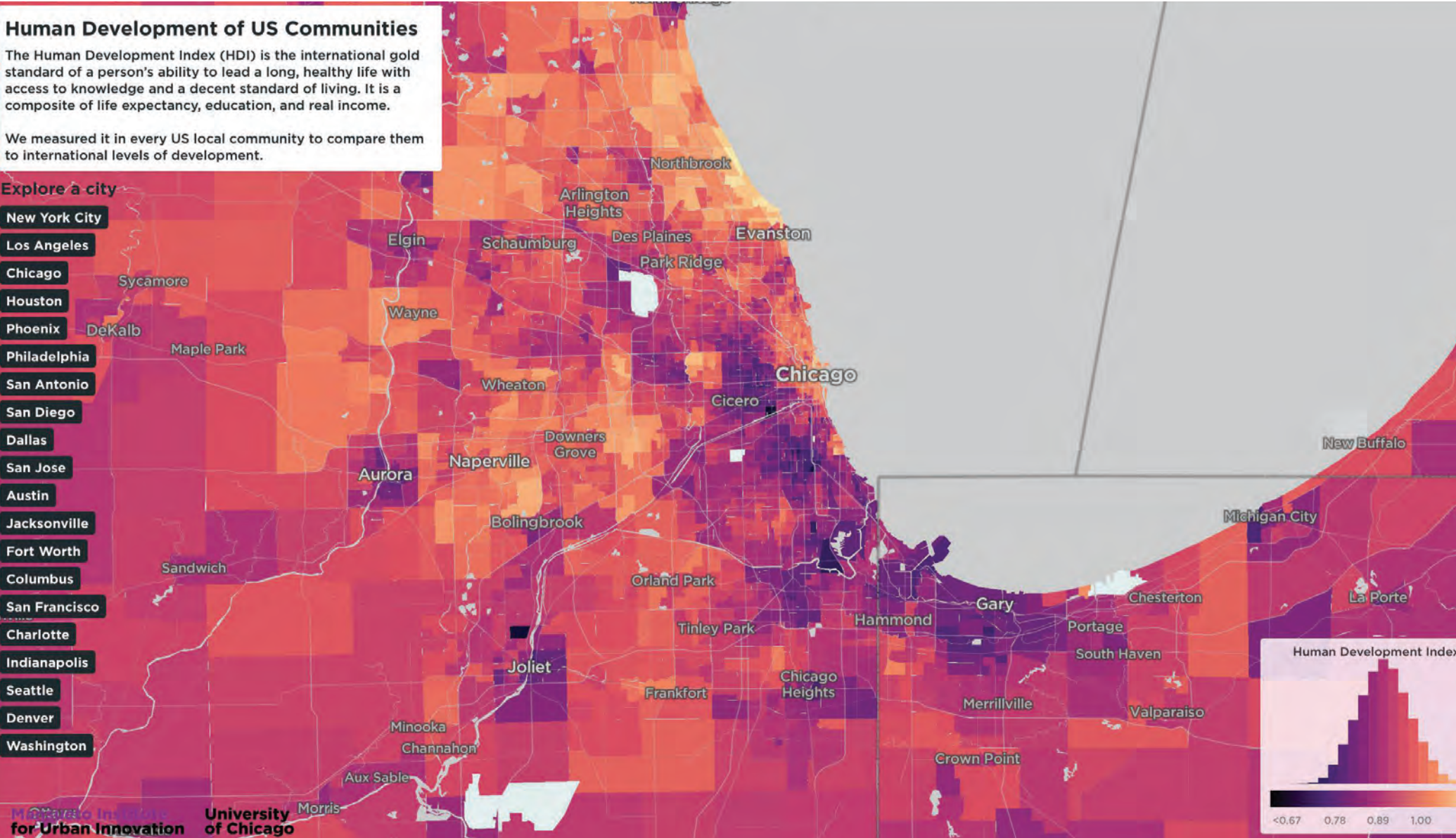
Human Development of US Communities

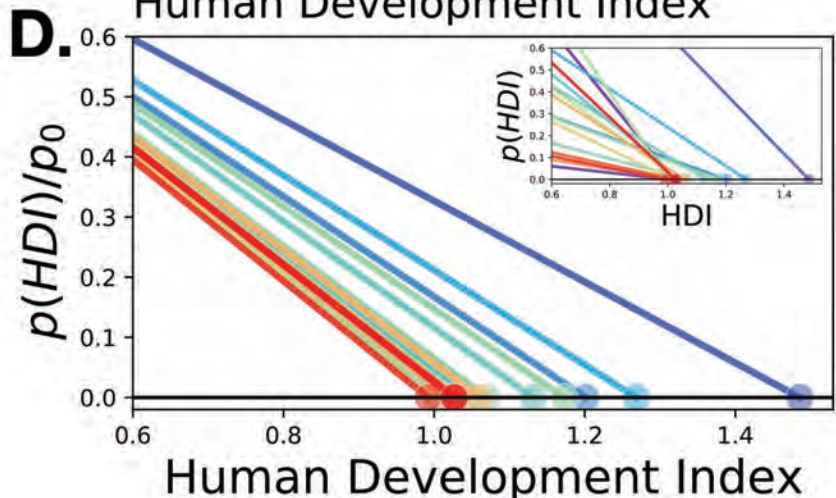
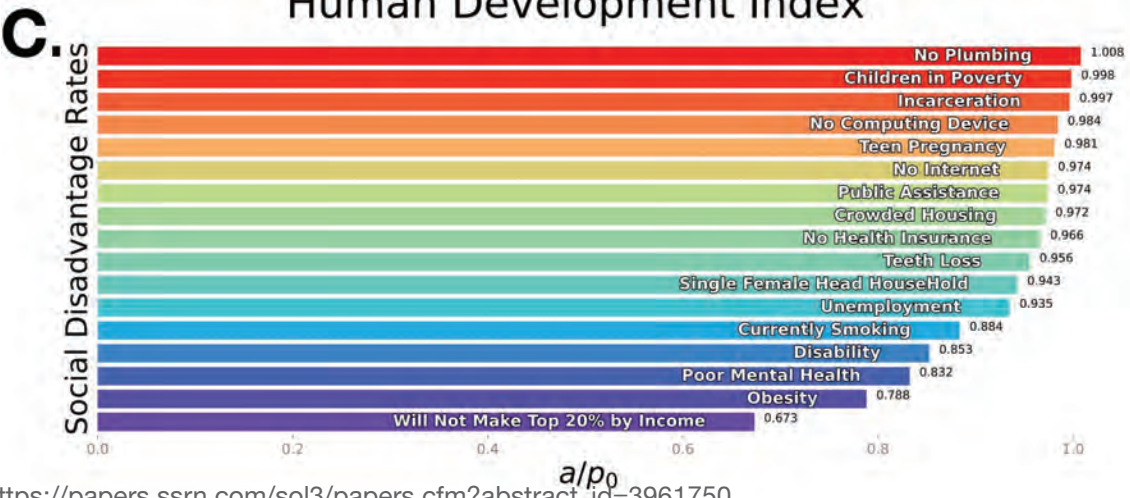
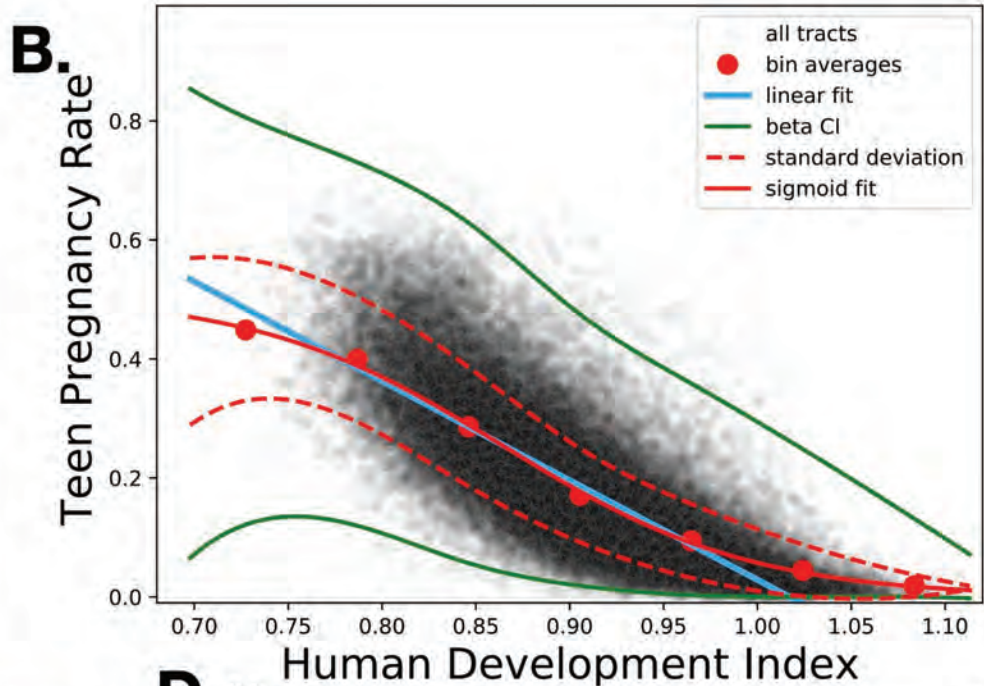
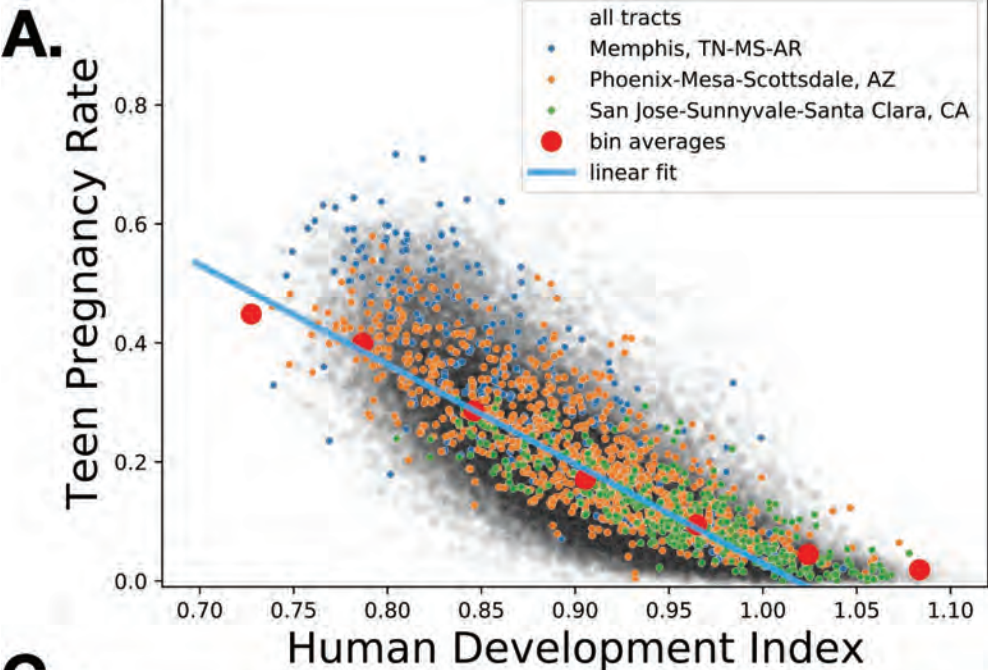
The Human Development Index (HDI) is the international gold standard of a person's ability to lead a long, healthy life with access to knowledge and a decent standard of living. It is a composite of life expectancy, education, and real income.

We measured it in every US local community to compare them to international levels of development.

Explore a city

- New York City
- Los Angeles
- Chicago
- Houston
- Phoenix
- Philadelphia
- San Antonio
- San Diego
- Dallas
- San Jose
- Austin
- Jacksonville
- Fort Worth
- Columbus
- San Francisco
- Charlotte
- Indianapolis
- Seattle
- Denver
- Washington





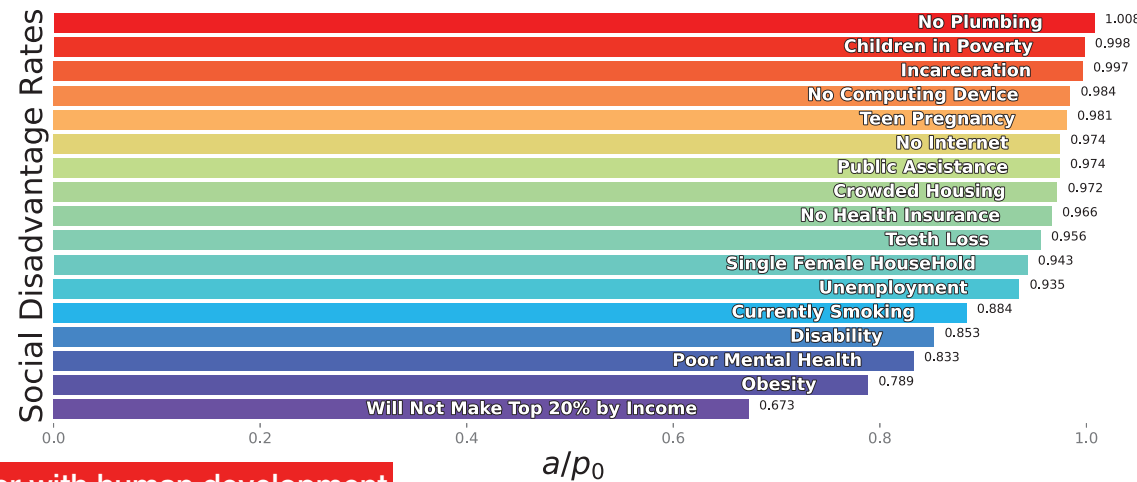
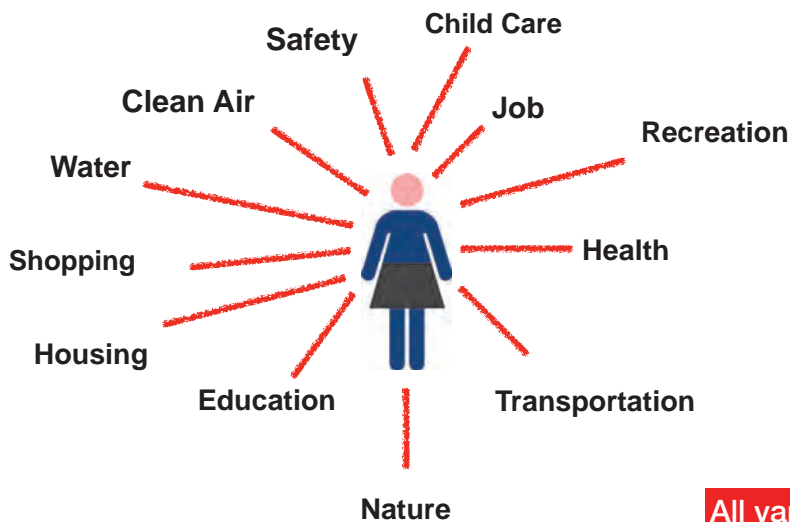
“Anna Karenina Principle” of Human Development

A deficiency in any **one of a number of factors** dooms an endeavor to failure.

Consequently, a successful endeavor (subject to this principle) is one for which every possible deficiency has been avoided.

https://en.wikipedia.org/wiki/Anna_Karenina_principle

All *high* human development communities are alike (“no problems”);
but each *low* human development community is challenged in its own way



All vary together with human development

Solution: ensure systemic human capabilities = education *and* health *and* decent real income

Human development as a network process (in cities)

2. Incipient city networks and spatial network development

can we accelerate it, and make it better?



Christa Brelsford



Toward cities without slums: Topology and the spatial evolution of neighborhoods

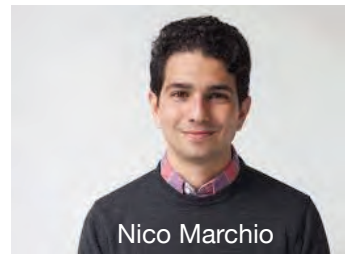
CHRISTA BRELSFORD, TAYLOR MARTIN, JOE HAND, AND LUÍS M. A. BETTENCOURT

SCIENCE ADVANCES • 29 Aug 2018 • Vol 4, Issue 8 • DOI: 10.1126/sciadv.aar4644

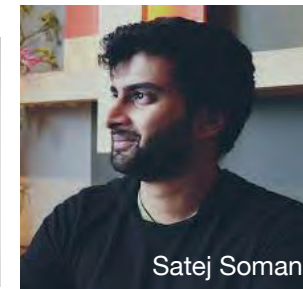
4,516

Abstract

The world is urbanizing quickly with nearly 4 billion people presently living in urban areas, about 1 billion of them in slums. Achieving sustainable development from rapid urbanization relies critically on creating cities without slums. We show that it is possible to diagnose systematically the central physical problem of slums—the lack of spatial accesses and related services—using a topological analysis of neighborhood maps and resolved by finding solutions to a sequence of constrained optimization problems. We set up the problem by showing that the built environment of any city can be decomposed into two types of networked spaces—accesses and places—and prove that these spaces display universal topological characteristics. We then show that while the neighborhoods of developed cities express the same common topology, urban slums fall into a different topological class. We demonstrate that it is always possible to find solutions that grow a street network in existing slums, providing universal accesses at minimal disruption and cost. We then show how elaborations of this procedure that include local preferences and reduce travel distances between places result from additional access construction. These methods are presently taking effect in neighborhoods in Cape Town (South Africa) and Mumbai (India), demonstrating their practical feasibility and emphasizing their role as a platform to enable communities and local governments to combine technical knowledge with local aspirations into contextually appropriate urban sustainable development solutions.



Nico Marchio



Satej Soman



Cooper Nederhood



Open Access Editor's Choice Article

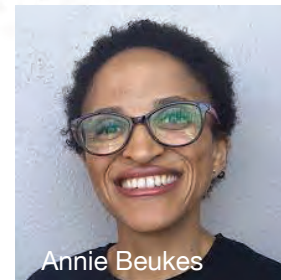
Worldwide Detection of Informal Settlements via Topological Analysis of Crowdsourced Digital Maps

by Satej Soman 1, Anni Beukes 1, Cooper Nederhood 1, Nicholas Marchio 1 and Luis M. A. Bettencourt 1,2,3

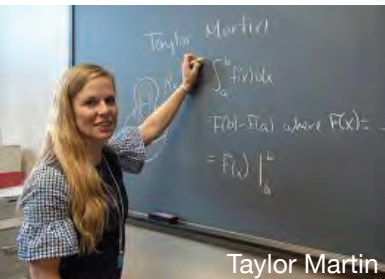
- 1 Mansueto Institute for Urban Innovation, University of Chicago, Chicago, IL 60637, USA
- 2 Department of Ecology and Evolution, University of Chicago, Chicago, IL 60637, USA
- 3 Department of Sociology, University of Chicago, Chicago, IL 60637, USA

* Author to whom correspondence should be addressed.

ISPRS Int. J. Geo-Inf. 2020, 9(11), 685; <https://doi.org/10.3390/ijgi9110685>



Annie Beukes



Taylor Martin

<https://www.science.org/doi/10.1126/sciadv.aar4644>



West Loop

West Loop Gate

Chicago Chicago

Printer's Row

Chicago Loop

Loop

New East Side

Millennium Park

Grant Park

Image NOAA
© 2018 Google

Google Earth

2000

41°53'05.55" N 87°38'09.31" W elev 1188 ft eye alt 3298 ft



© 2018 AfriGIS (Pty) Ltd.

Google Earth

2005

34°03'43.43" S 18°40'19.20" E elev 142 ft eye alt 317 ft

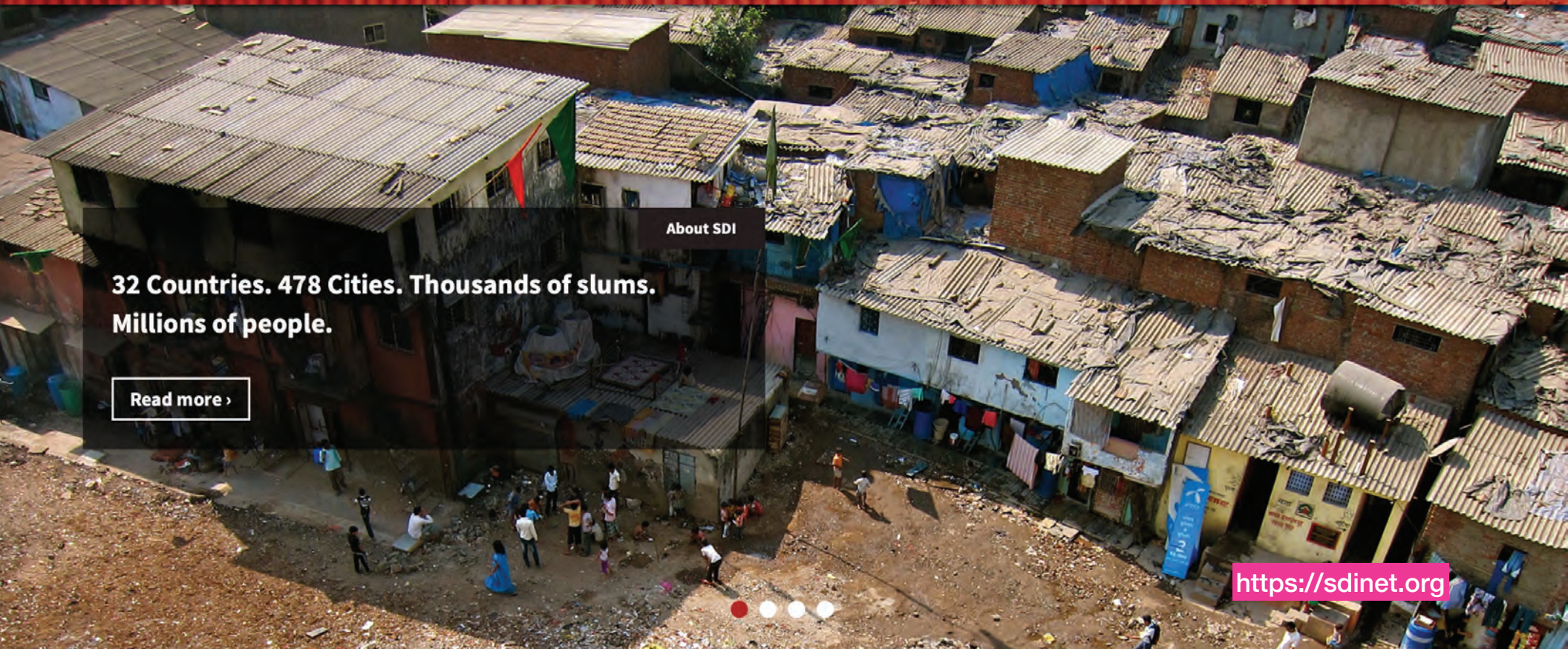


EXPLORE OUR DATA

BLOG

RESOURCES

MULTIMEDIA



About SDI

**32 Countries. 478 Cities. Thousands of slums.
Millions of people.**

Read more ›

<https://sdinet.org>



Sanitation

Working toilet seats to people:
1:18,326

Number of working toilets seats:



Total number of toilets seats:
2

Types of toilets in use:

- Flush
- ✓ **Pour flush**
- Ecosan
- Chemical
- ✓ **Pit latrine**
- Hanging toilet
- Flush

Organised Community

Number of savings groups:
18

Community leadership?
Yes

How often does the community meet?
Other

Does the community leadership talk to the city?
N/A

Relationship with authorities:
Good

How often does the community meet with the city?
Monthly

Water

Number of taps:
9

Number of working taps:



Working taps to people:
1:4,072

Average cost of access per month:
50,000 SLL

Most common diseases:

- **Malaria**
- **Typhoid**
- **Diarrhea**
- **Other**

Access to health clinics:
Yes

Average walking time to nearest health clinic (minutes):
Unknown

Access to AIDS clinics:
Yes

Average walking time to nearest Aids clinic (minutes):
30 minutes to 1 hour

Access to hospitals:
Yes

Average walking time to nearest hospital (minutes):
more than 1 hour

Health Access

Mapping households is very slow and labor intensive

Infrastructure

Electricity available:
Yes

Garbage collections per week:
N/A

Garbage location:
Common area inside settlement

Road types:
Gravel roads

Main means of transportation:

- ✓ **Bus**
- ✓ **Motorbike**
- Car**
- Bicycle**
- Train**
- Walking**
- Tandem**
- Ox cart**

Commercial Establishments & Facilities

- ✓ **Playground**
- ✓ **General shops**
- ✓ **Furniture shops**
- ✓ **Communications**
- Banks**
- ✓ **Informal markets**
- ✓ **Temples**
- ✓ **Car repair**
- Firestations**
- ✓ **Food shops**
- Mosques**
- ✓ **Police stations**
- Clothing shops**
- ✓ **Churches**

<https://knowyourcity.info>

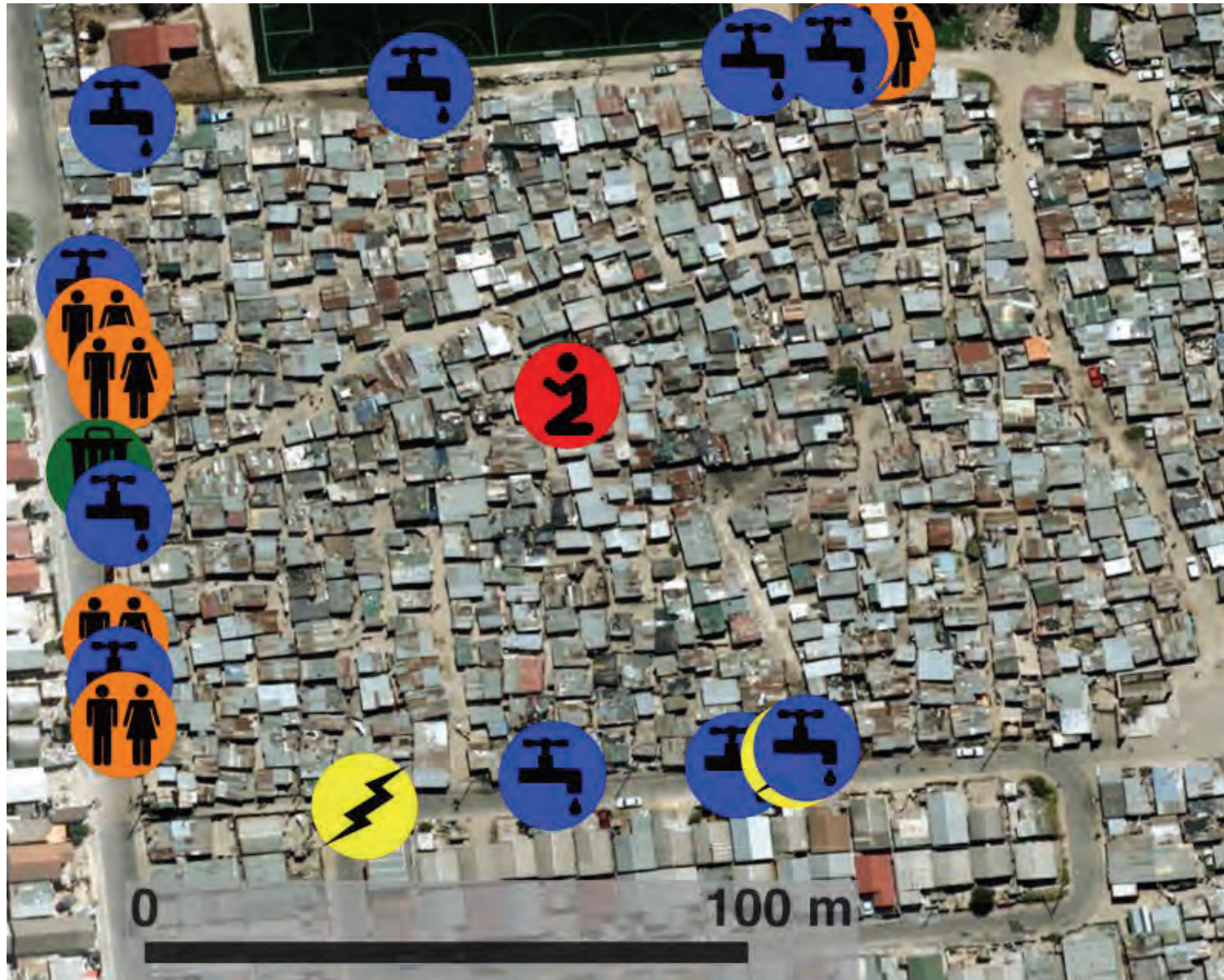
Old Fadama, Accra, Ghana



Street

Reblocking !

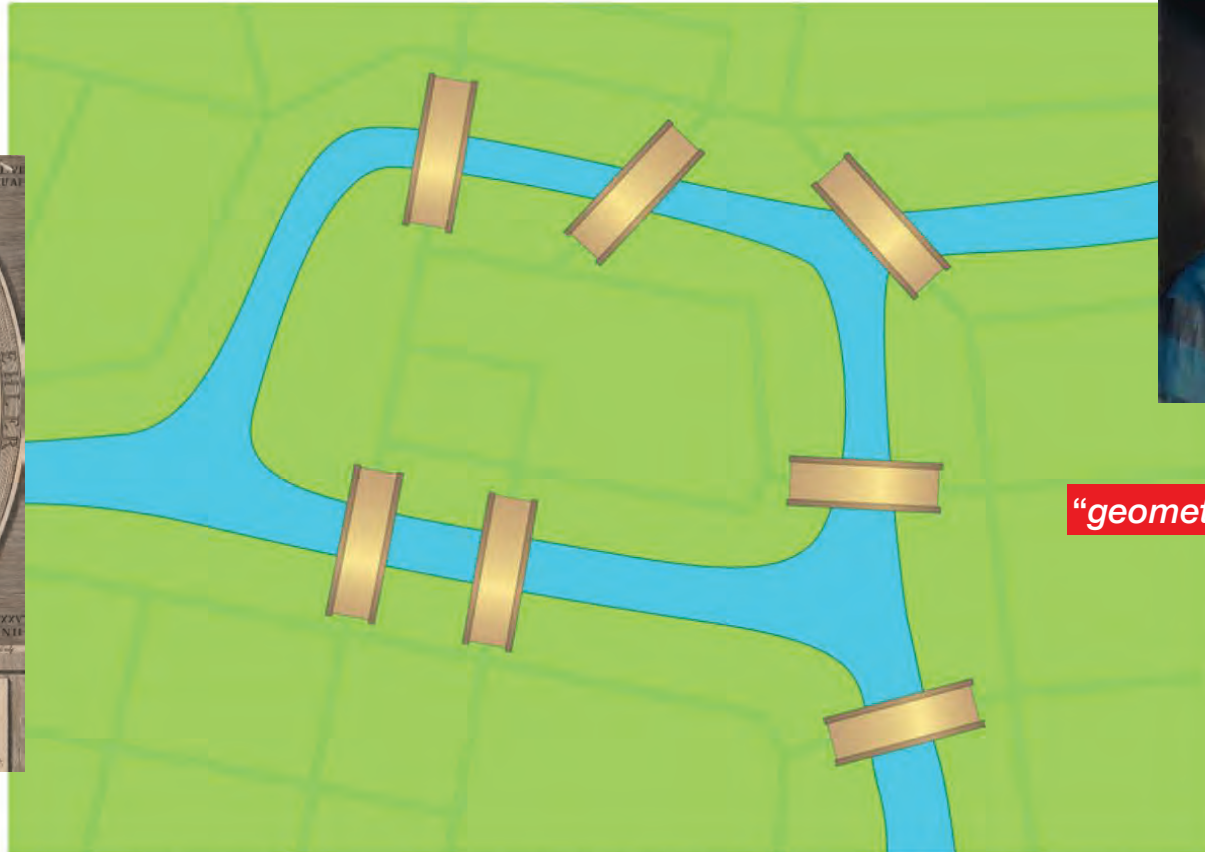
Every building gets street access, an address, services.



“This question is so banal, but seemed to me worthy of attention in that [neither] geometry, nor algebra, nor even the art of counting was sufficient to solve it.”



Kart Gottlieb Ehler



Leonard Euler

“geometria situs” → topology

The Königsberg Bridge problem asked whether it was possible for a person to walk through the city, crossing each bridge once and only once. Image credit: ScienceSource/SPL.

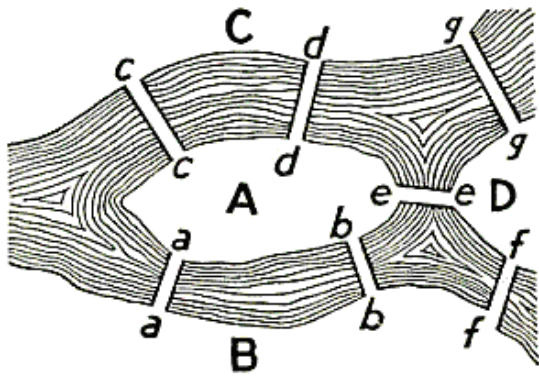


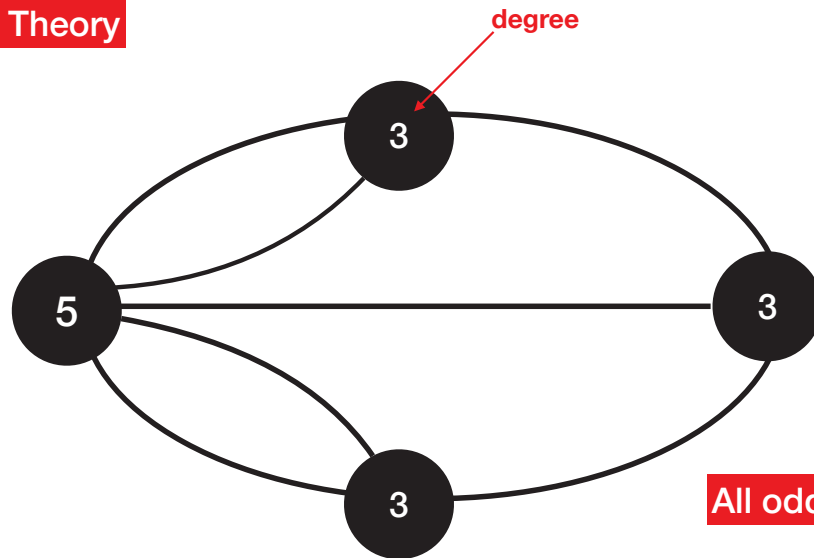
FIGURE 98. *Geographic Map:
The Königsberg Bridges.*



number of bridges must be even, except at starting and finishing points

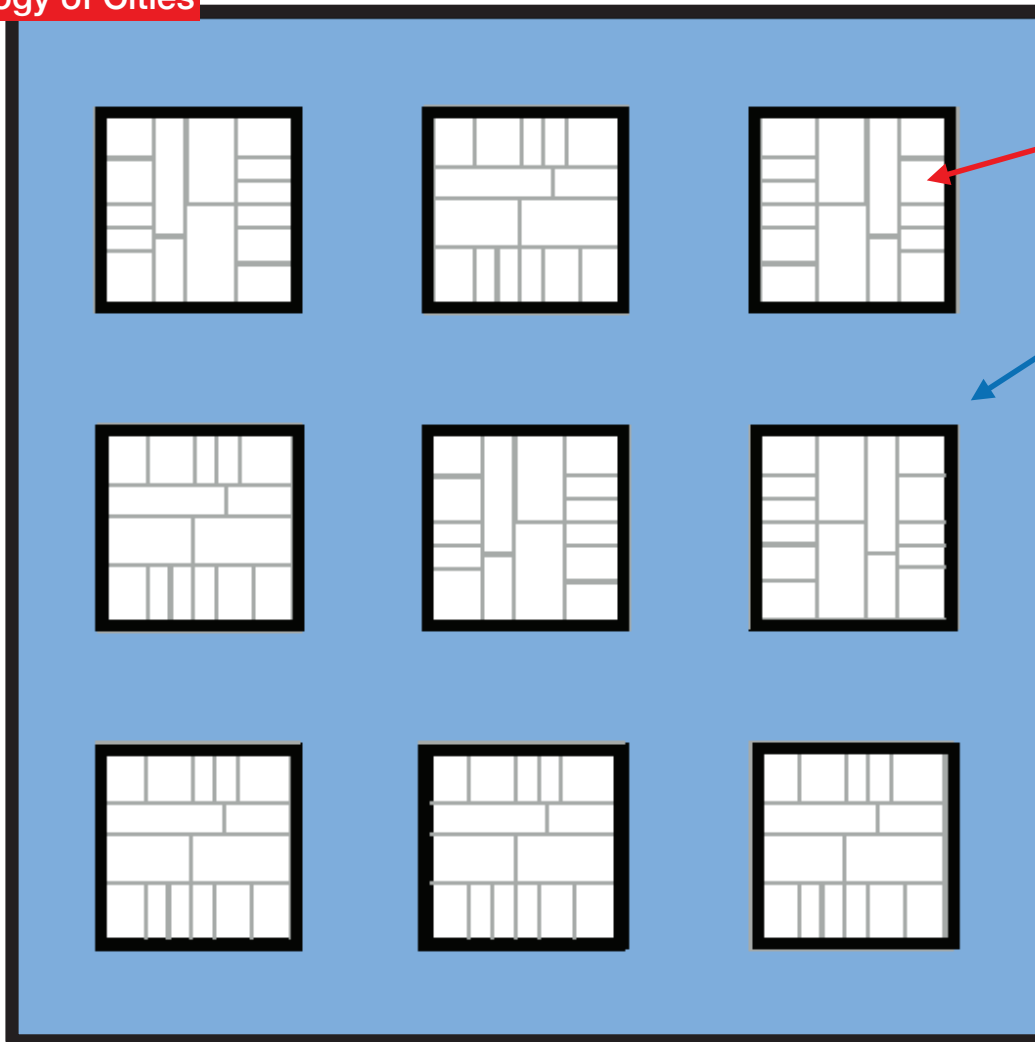
<https://mathworld.wolfram.com/KoenigsbergBridgeProblem.html>

Geometry —> Topology —> Graph Theory



All odd degree: Eulerian circuit is not possible !

The General Topology of Cities



Buildings (parcels)

Street Network

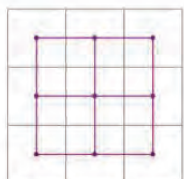
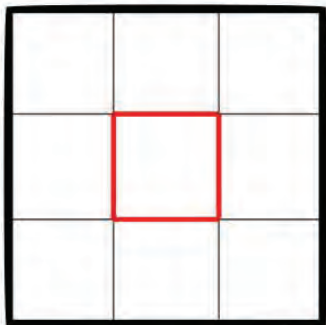
$$\chi = 1 - b$$

The Euler characteristic of a city with b blocks

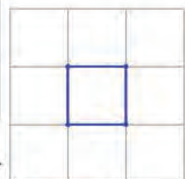
Equivalent to a disk with b holes

Every city is topologically like this, but geometry varies

A.
Lattice, S_0



S_1

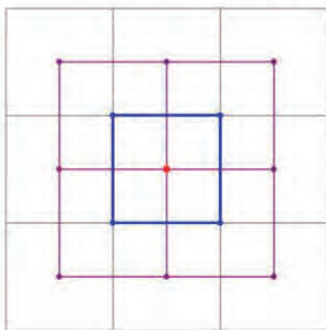


S_2

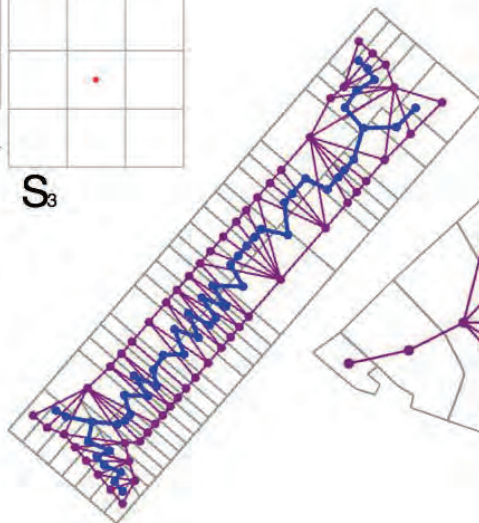
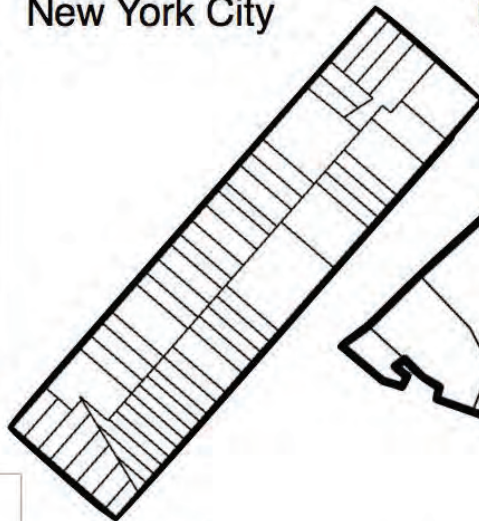


S_3

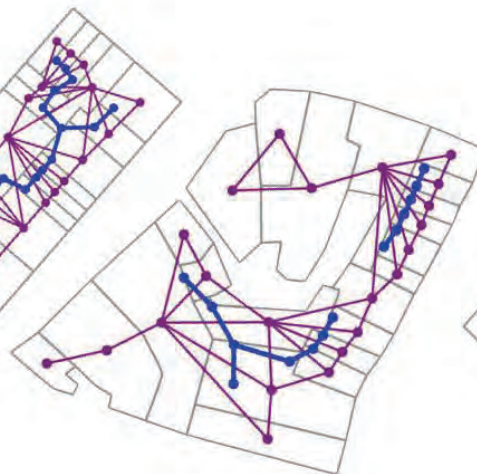
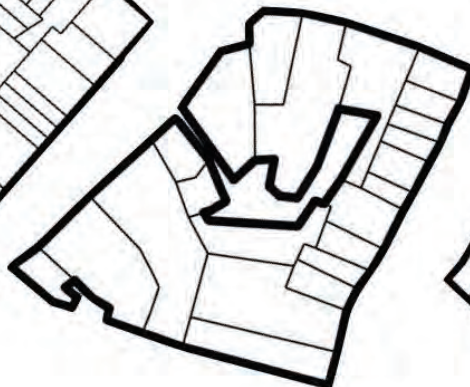
Weak dual graphs



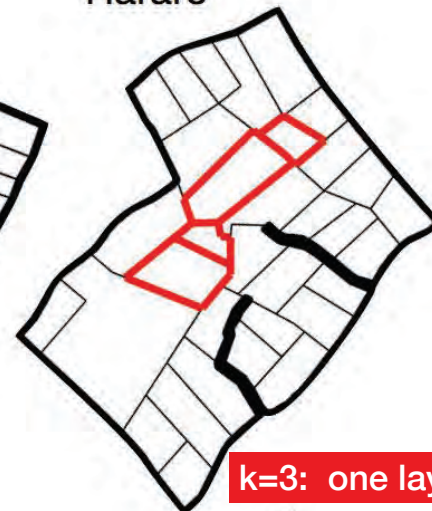
B.
New York City



C.
Prague

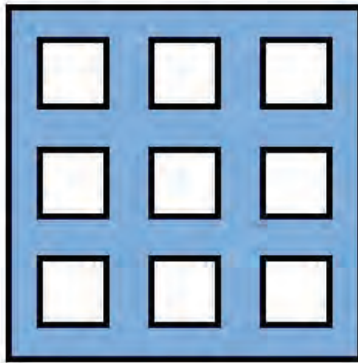


D.
Harare

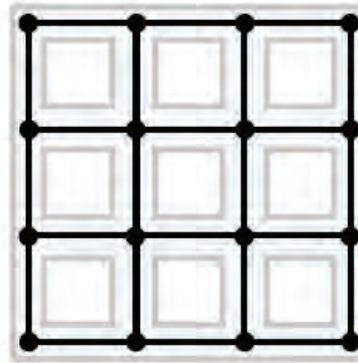


$k=3$: one layer in from street

City

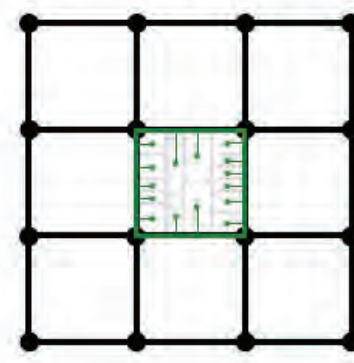


Access Space



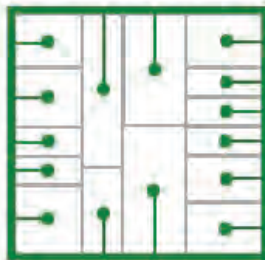
Access Network, Y

Blocks



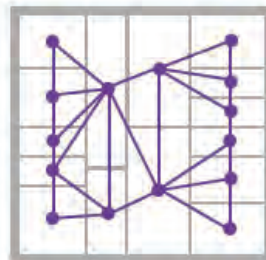
Bridge, X

Blocks

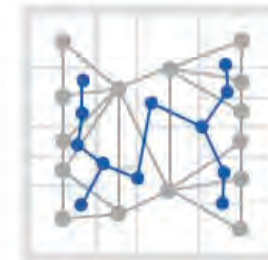


Bridge, X

Parcels

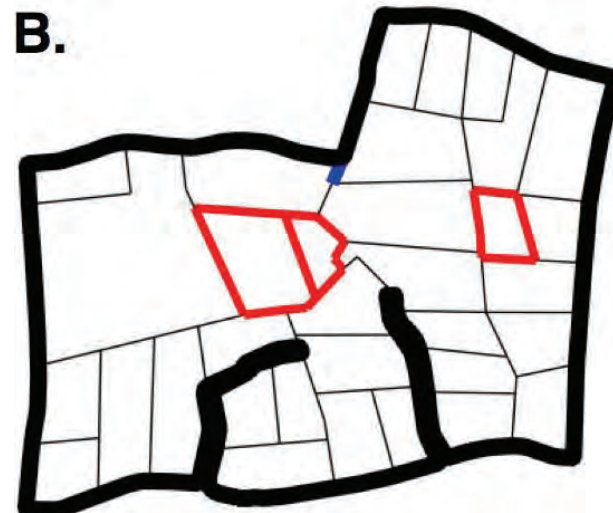
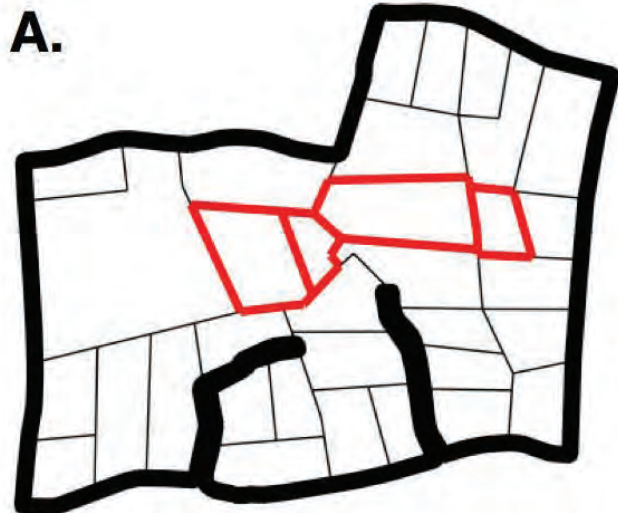


S₁

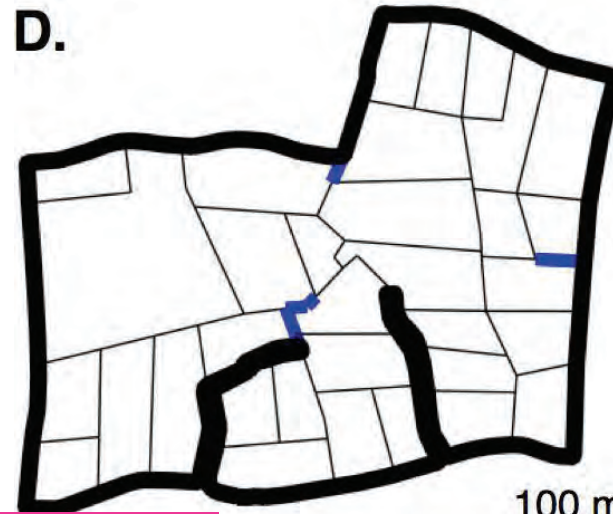
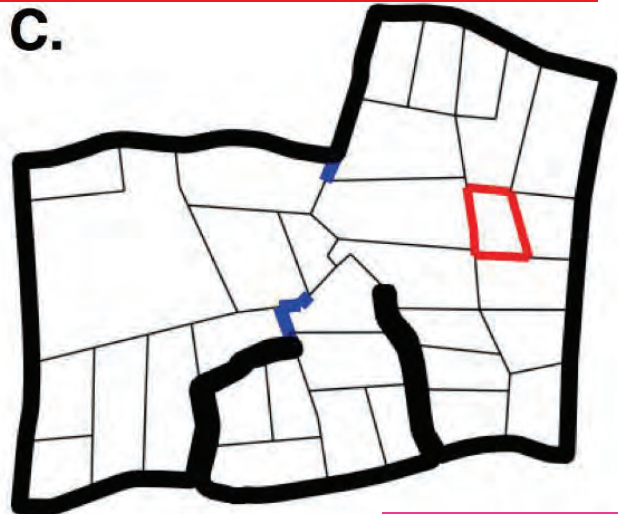


S₂

Algorithm for analyzing the topology of any city : And identify buildings without accesses

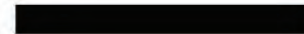


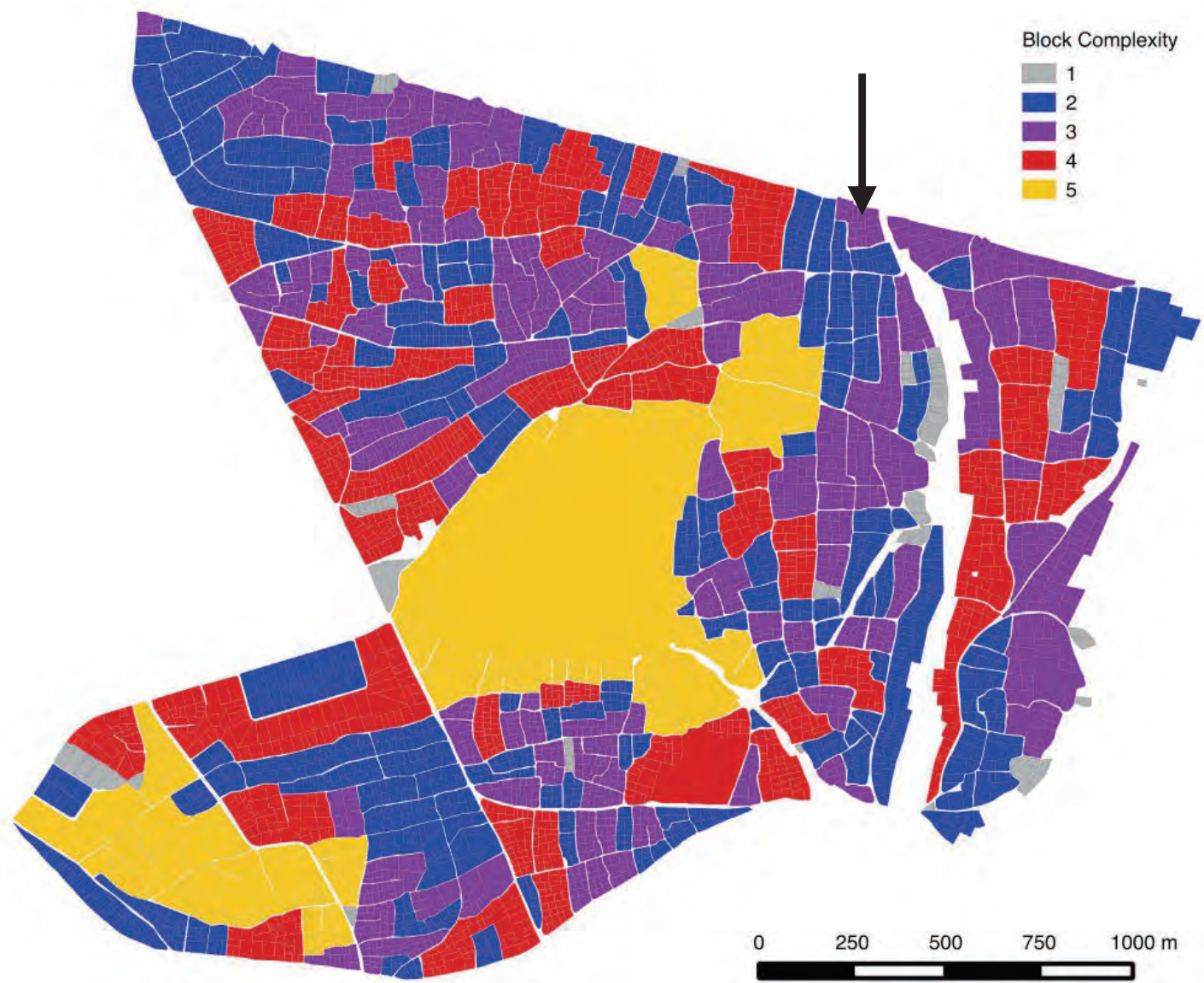
And estimate where minimal additional accesses may go



Steiner Tree Problem on block graph

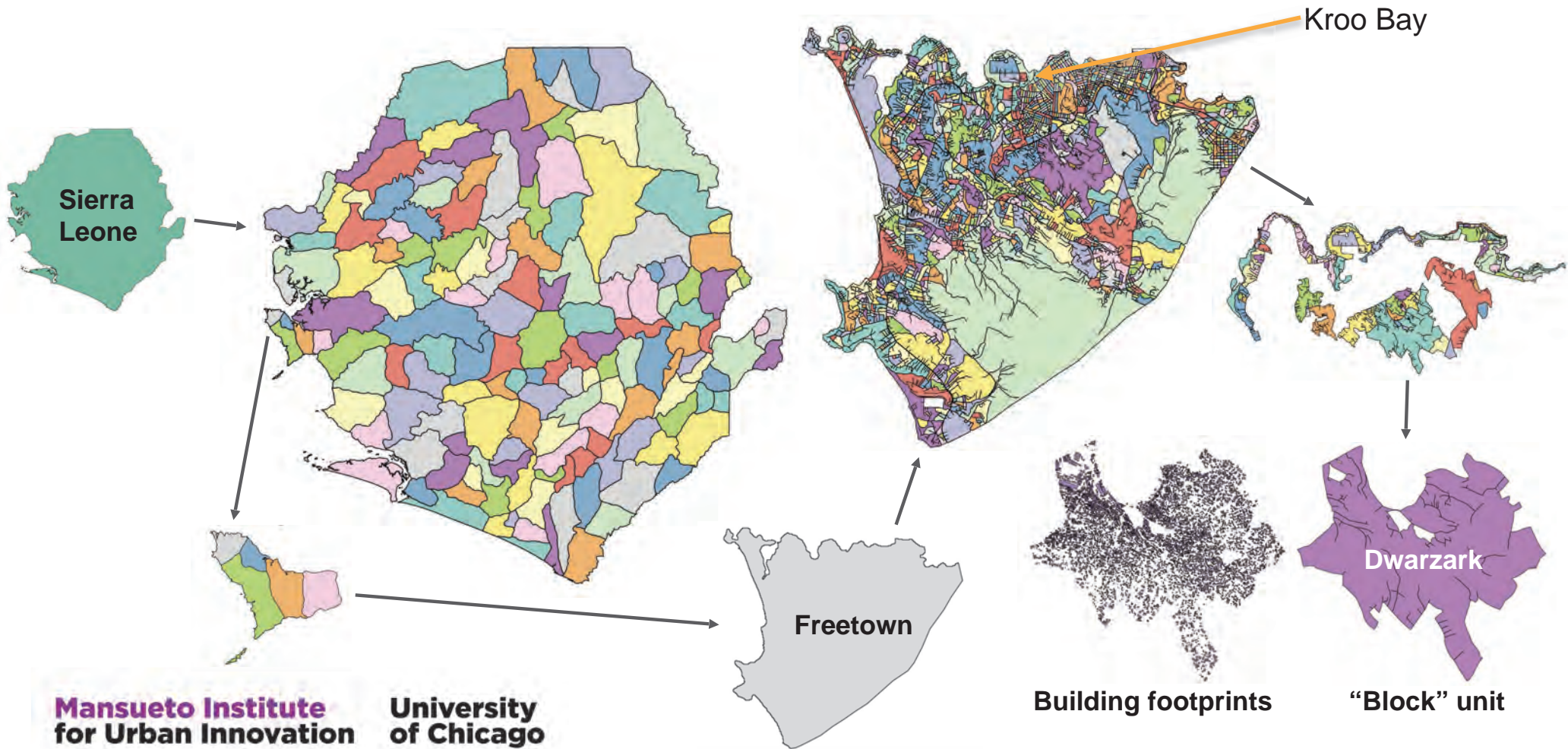
100 m





Understanding settlements from global to local scales

a global map (of cities) neighborhood by neighborhood



Detecting informality down to the street block

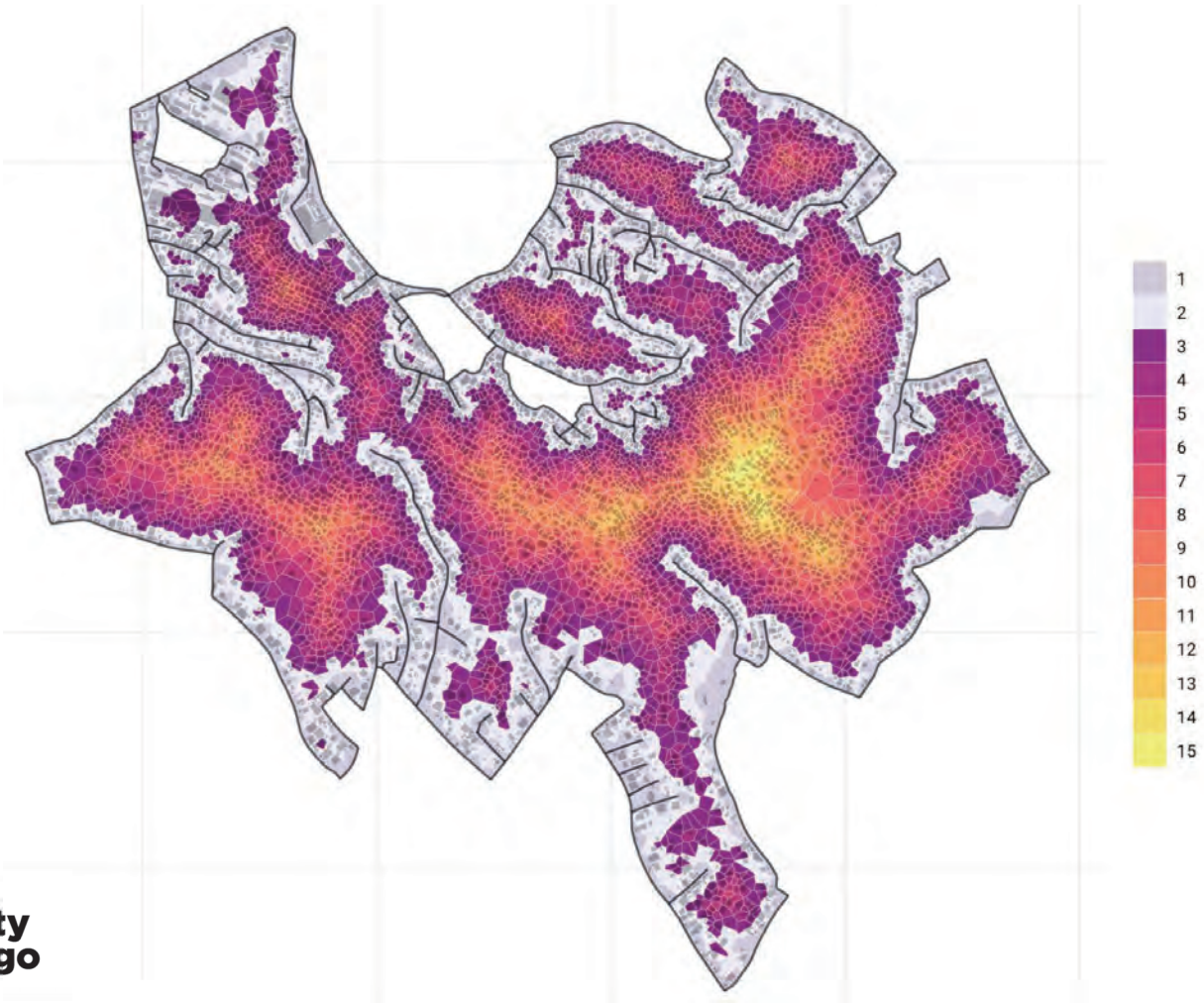


Building footprints



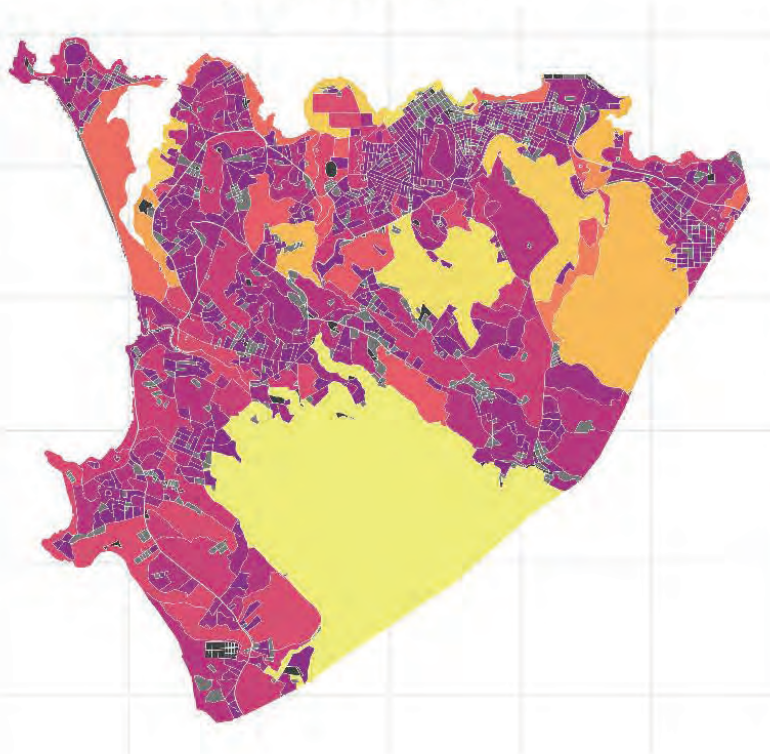
Dwarzark

“Block” unit



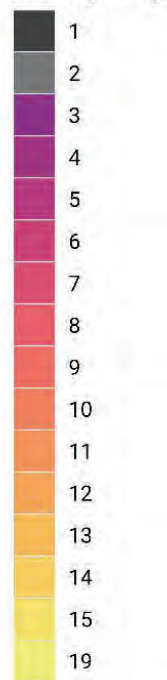
Mapping informality and population in Freetown

Informal settlements

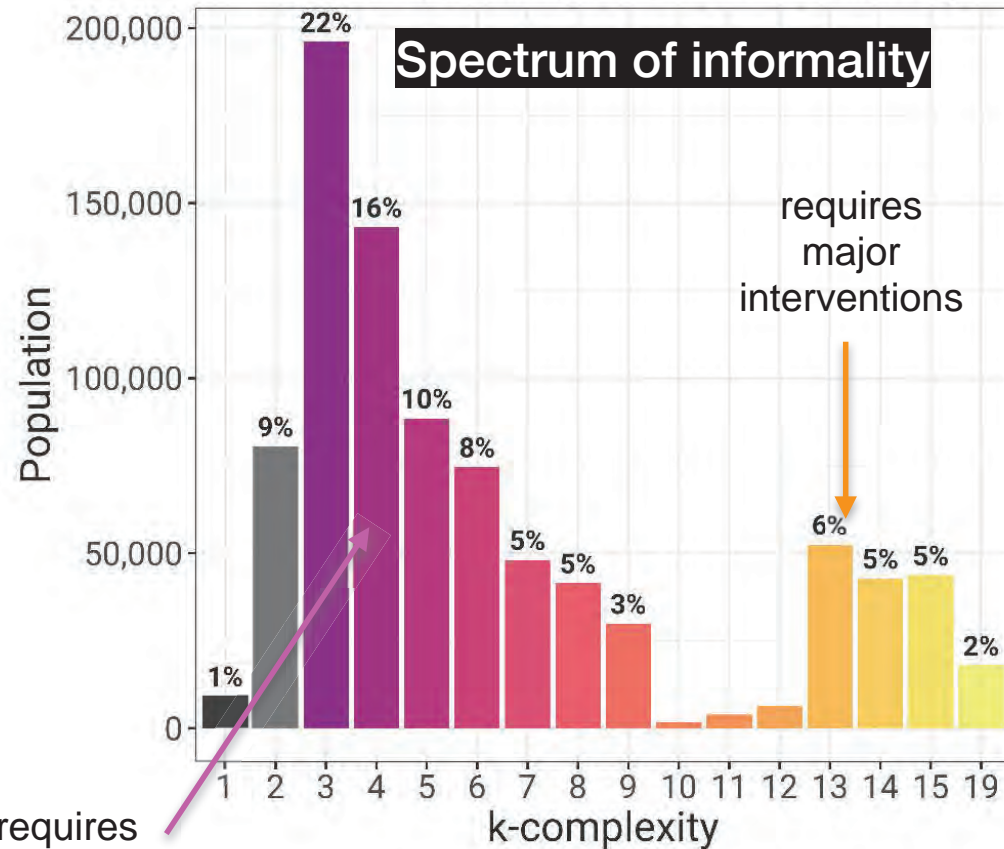


Total Population: 880,537

k-complexity



Population distribution across levels of informality

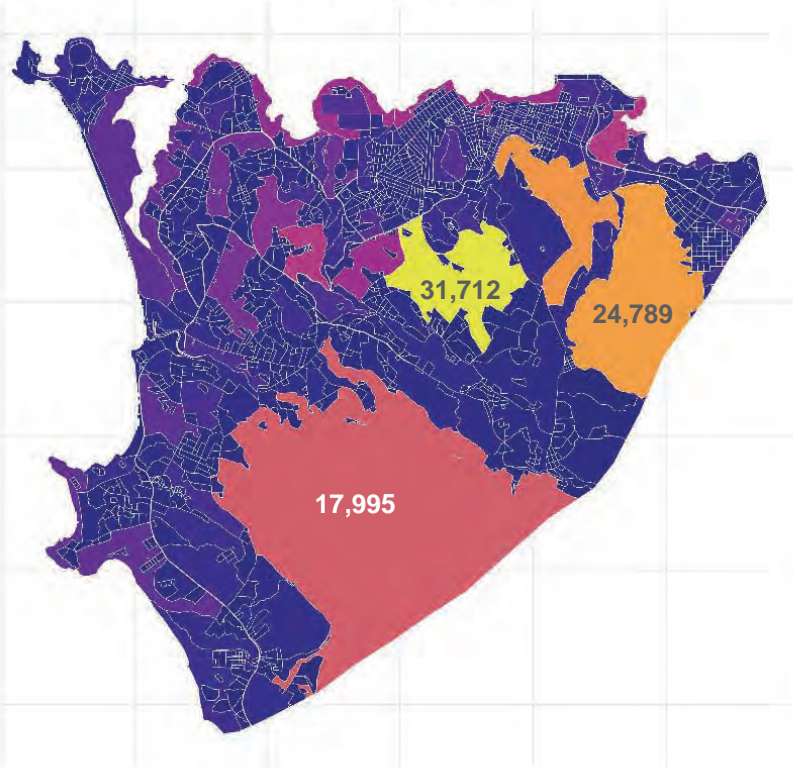


requires
minor extensions
of streets+services

requires
major
interventions

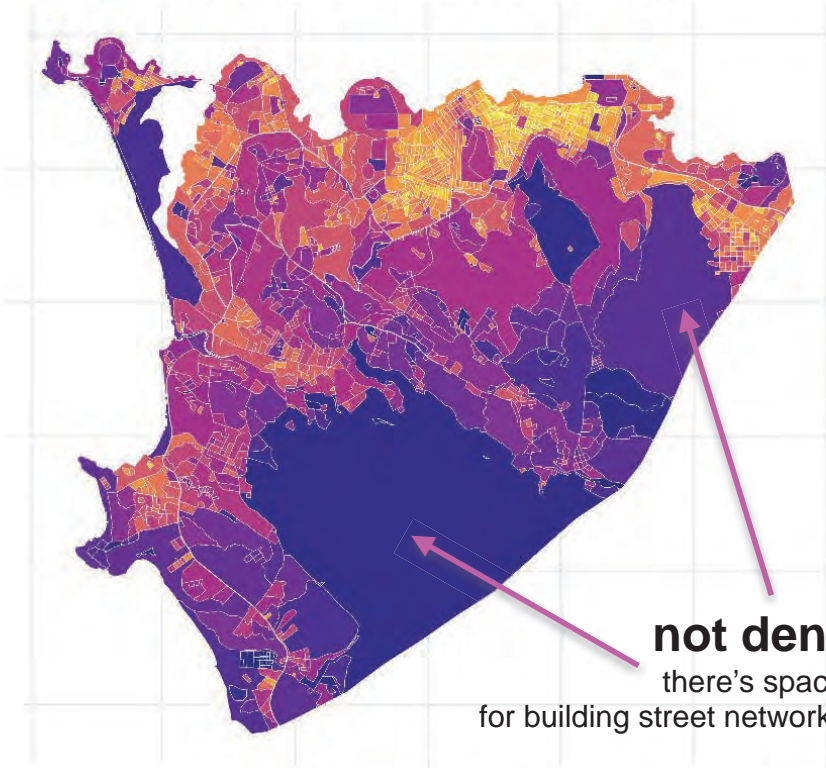
New indicators for measuring development in cities

Block Population



Total Population: 880,537

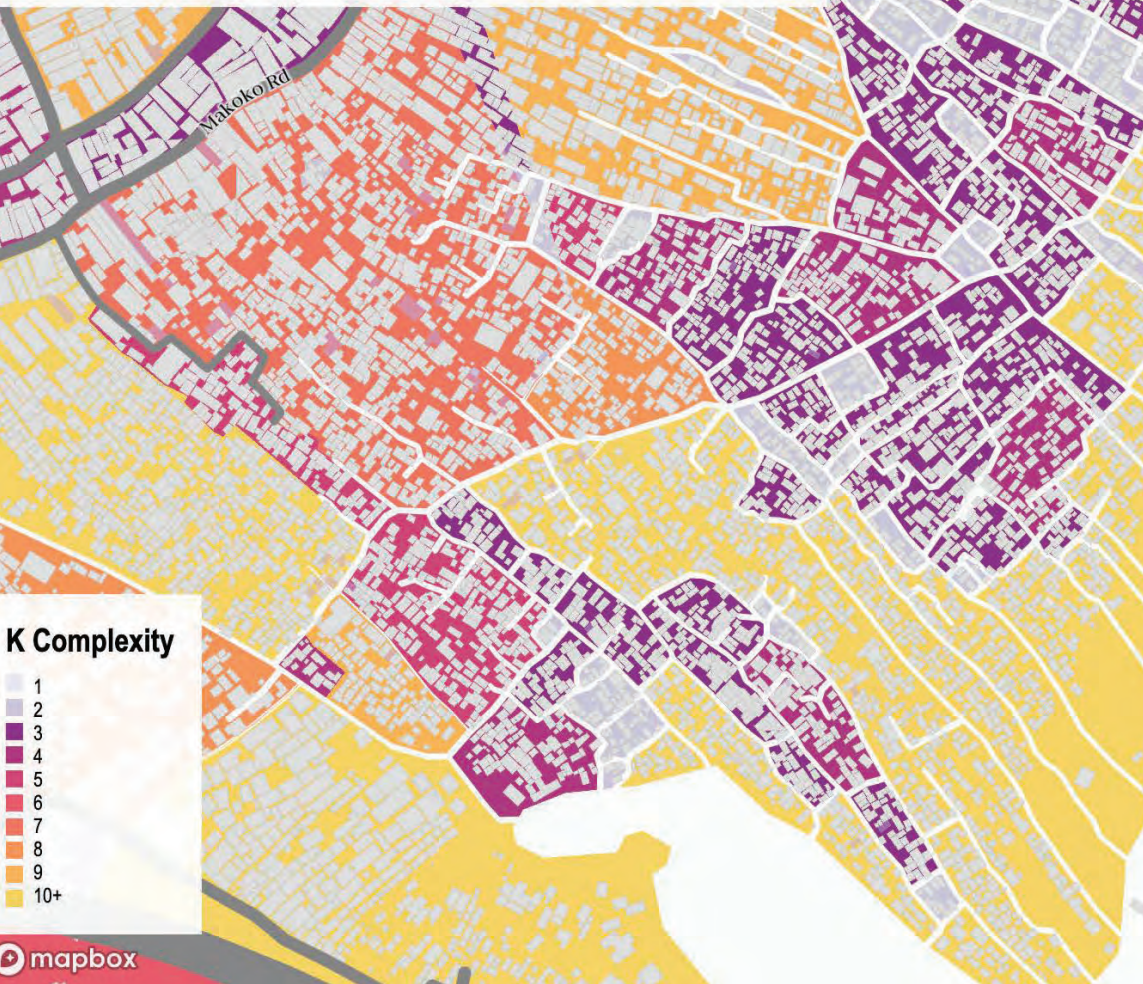
Proportion of area covered in buildings



Legend color scale is top-coded with max value of 100%

Million Neighborhoods Data Explorer

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To take up this project, young residents of Makoko were taught to pilot drones and populate the map with images from the community. Hounkpe is one of the residents on the project that is also teaching residents how to fly drones.

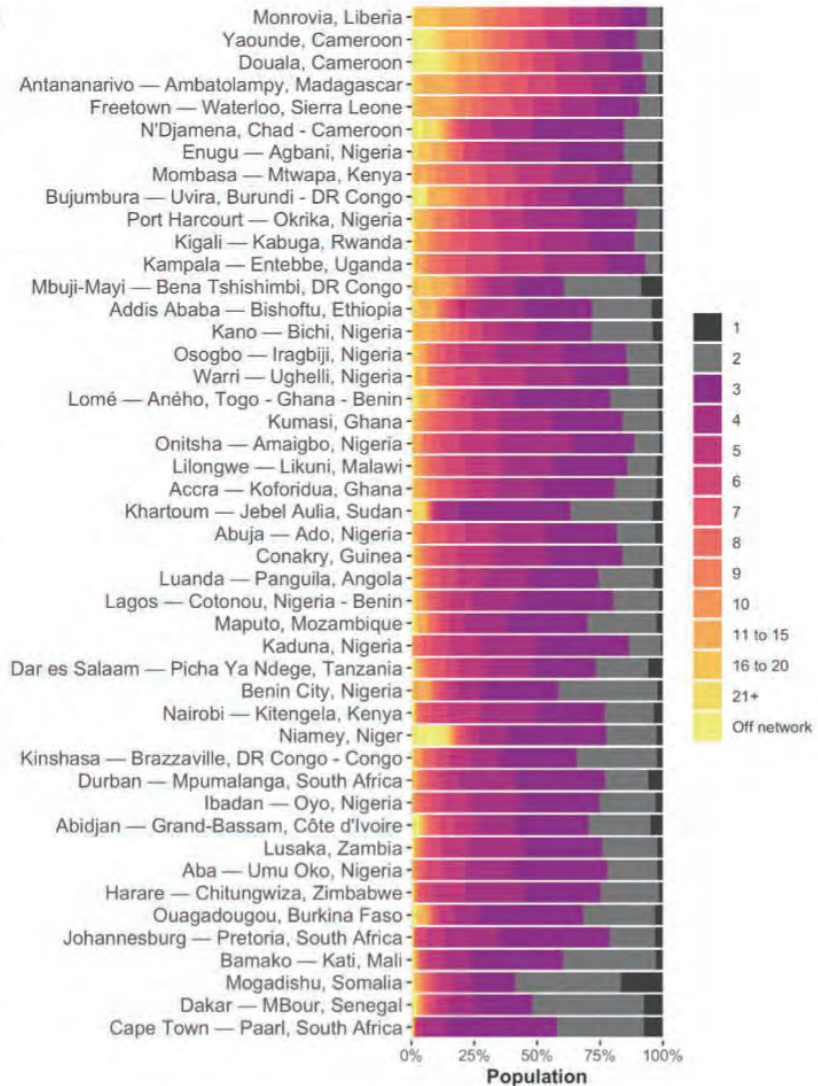
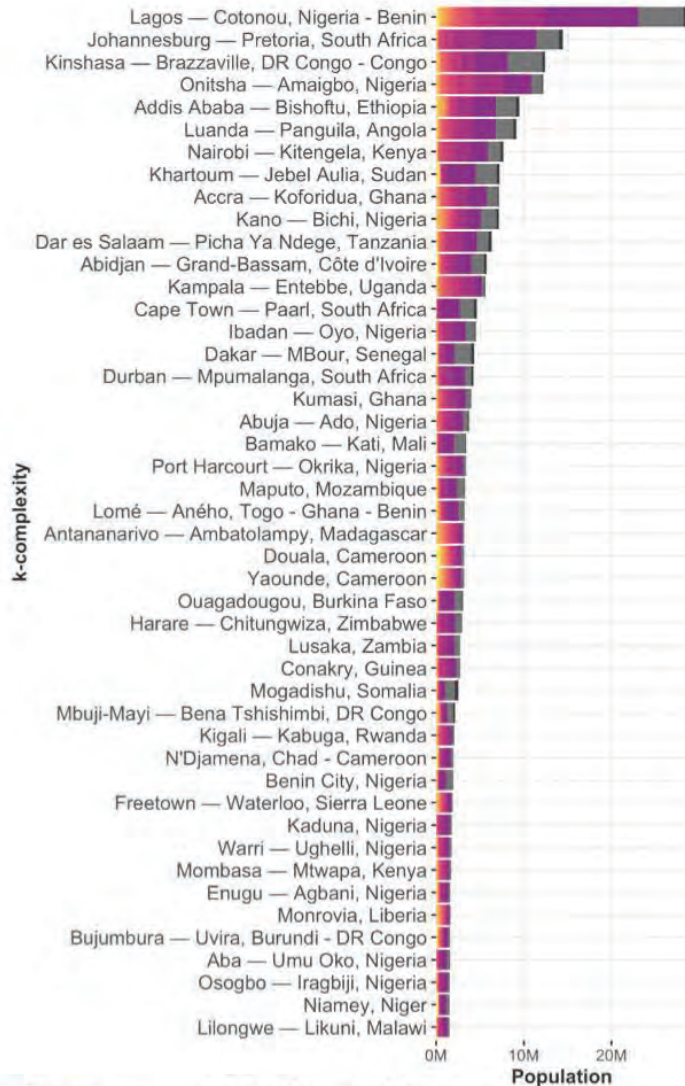


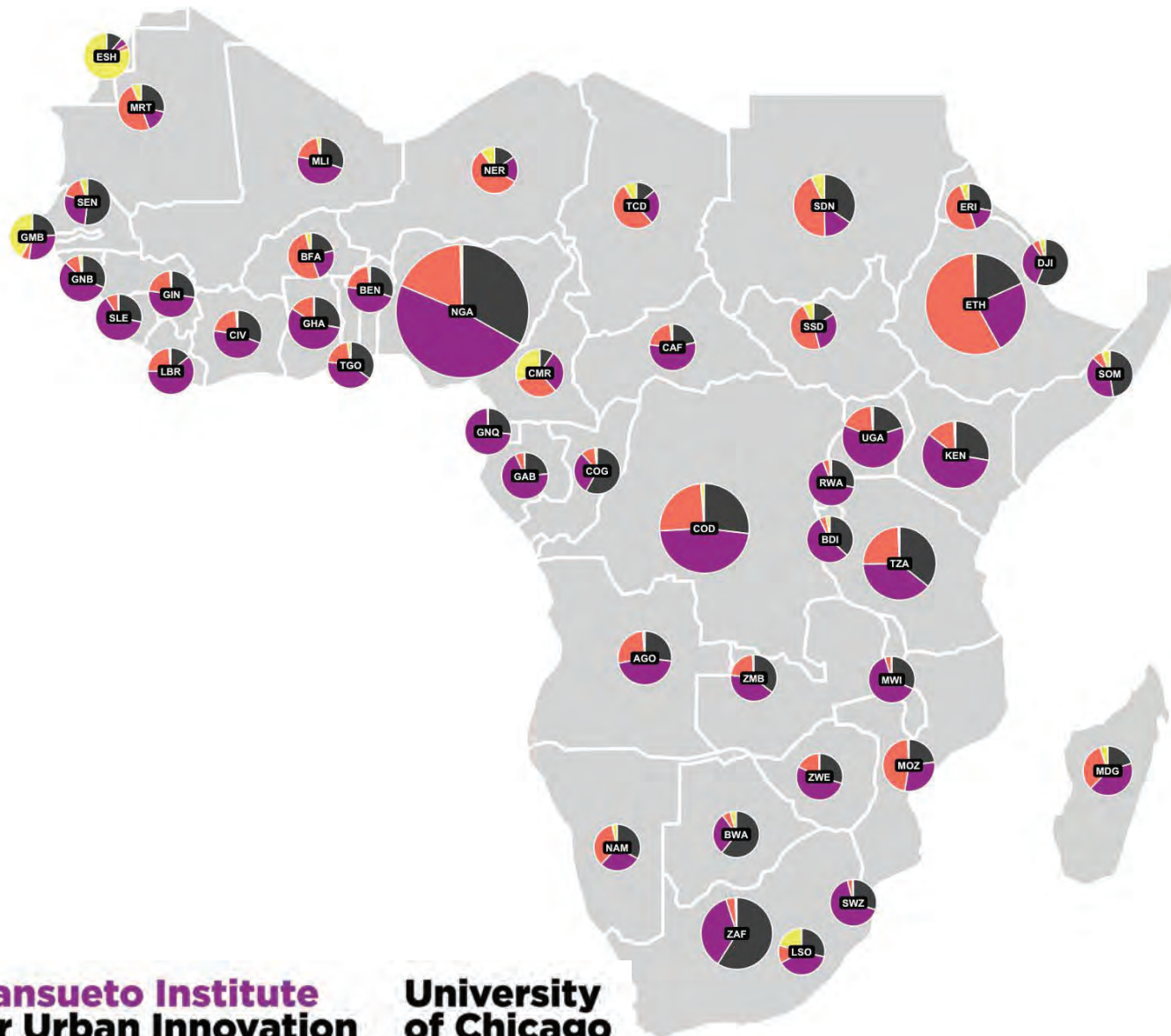
YASUYOSHI CHIBA/AFP/Getty Images

A classroom session at a private school in the Makoko on March 1, 2019.

“For years, Makoko has been ignored by governments of the state. This project is the first part of a conversation around inclusion. We are helping map out Makoko so that governments and other organizations can provide interventions and access to social services like electricity, healthcare, and education.” Ottaviani told CNN.

<https://www.cnn.com/2020/02/26/africa/nigeria-makoko-mapping-intl/index.html>



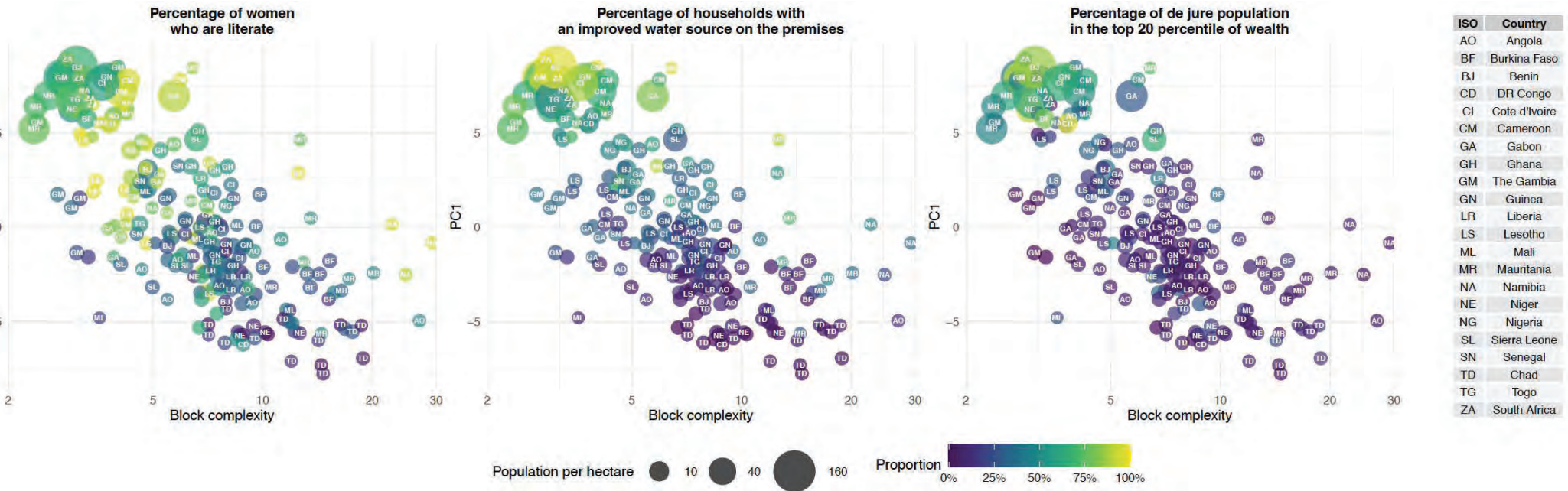


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... to the continent.

Human development and connectivity



ISO	Country
AO	Angola
BF	Burkina Faso
BJ	Benin
CD	DR Congo
CI	Cote d'Ivoire
CM	Cameroon
GA	Gabon
GH	Ghana
GM	The Gambia
GN	Guinea
LR	Liberia
LS	Lesotho
ML	Mali
MR	Mauritania
NA	Namibia
NE	Niger
NG	Nigeria
SL	Sierra Leone
SN	Senegal
TD	Chad
TG	Togo
ZA	South Africa

From international human and health surveys

Thank you !

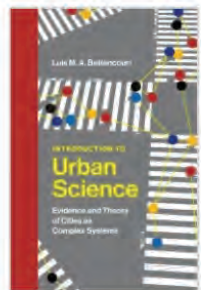
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