

SFI-CSSS, 6th July 2023 page 1 of 17

The Team

The Physicists





Al special-ops





The Mathematician



The Economist



SFI-CSSS, 6th July 2023 page 2 of 17

What is the Collatz-Conjecture again?

The problem that even fifth graders can understand

But no one can solve...

SFI-CSSS, 6th July 2023 page 3 of 17

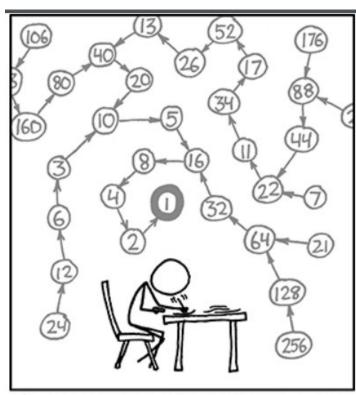
What is the Collatz-Conjecture again?

Pick any positive integer *n* and

$$f(n) = \begin{cases} n/2 & \text{if n is even} \\ 3n+1 & \text{if n is odd} \end{cases}$$

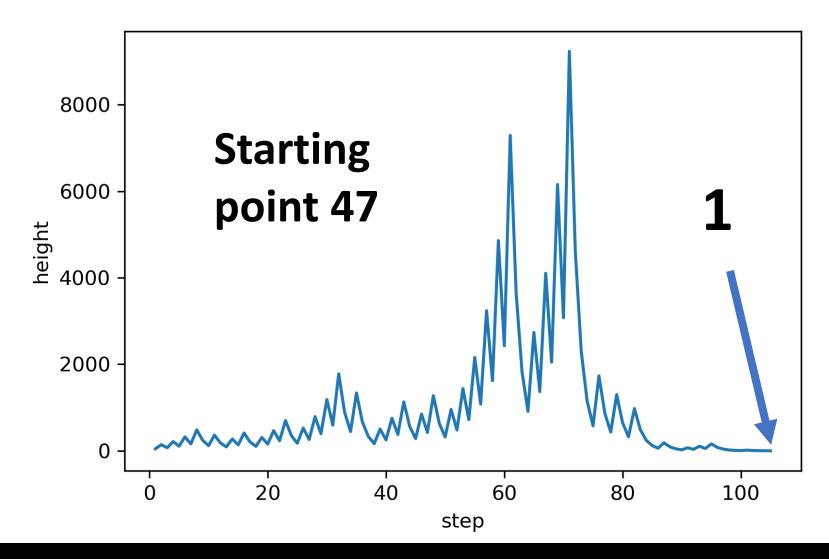
What is the Collatz-Conjecture again?

Your friends will stop calling you..



THE COLLATZ CONJECTURE STATES THAT IF YOU PICK A NUMBER, AND IF IT'S EVEN DIVIDE IT BY TWO AND IF IT'S ODD MULTIPLY IT BY THREE AND ADD ONE, AND YOU REPEAT THIS PROCEDURE LONG ENOUGH, EVENTUALLY YOUR FRIENDS WILL STOP CALLING TO SEE IF YOU WANT TO HANG OUT.

Collatz - An example



SFI-CSSS, 6th July 2023 page 6 of 17

What is it about 47 that it goes round like this?

Why work on this stuff?

Article

Advancing mathematics by guiding human intuition with AI

https://doi.org/10.1038/s41586-021-04086-x

Received: 10 July 2021

Accepted: 30 September 2021

Published online: 1 December 2021

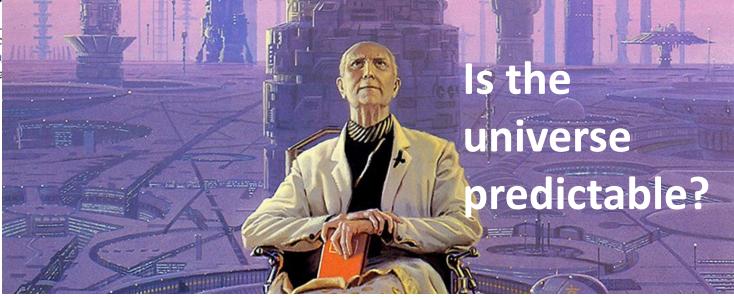
Open access

Check for updates

Alex Davies^{1, 1, 1}, Petar Veličković¹, Lars Buesing¹, Sam Blackwell¹, Daniel Zheng¹, Nenad Tomašev¹, Richard Tanburn¹, Peter Battaglia¹, Charles Blundell¹, András Juhász²,

Marc Lackenby², Geordie Williamson³, Demis

The practice of mathematics involves disc formulate and prove conjectures, resultin mathematicians have used computers to a



Initial discussions (1)



If we sufficiently characterize the numbers, AI can predict the trajectory length!

SFI-CSSS, 6th July 2023 page 9 of 17

Characterizing initial conditions = gathering data

$\begin{array}{cccccccccccccccccccccccccccccccccccc$					
Starting point	Even?	Odd?	Divisble by 3?	Prime?	Total stopping time (T)
1	0	1	0	0	
2	1	0	0	1	
3	0	1	1	1	
4	1	0	0	0	
5	0	1	0	1	
6	1	0	1	0	

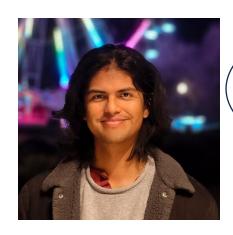
SFI-CSSS, 6th July 2023 page 10 of 17

That doesn't make any sense!



SFI-CSSS, 6th July 2023 page 11 of 17

Initial discussions (2)



I want to try!

There must be some information!

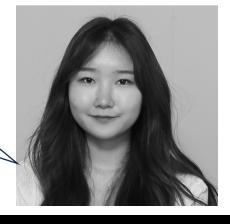
Walk the trajectory to predict it!



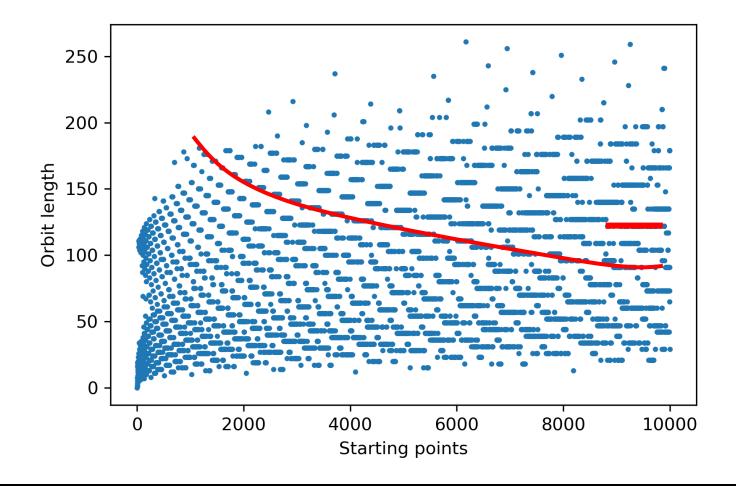
Stochasticity and distributions!



Reduce the dimensionality of the data



Clustering the other way around!

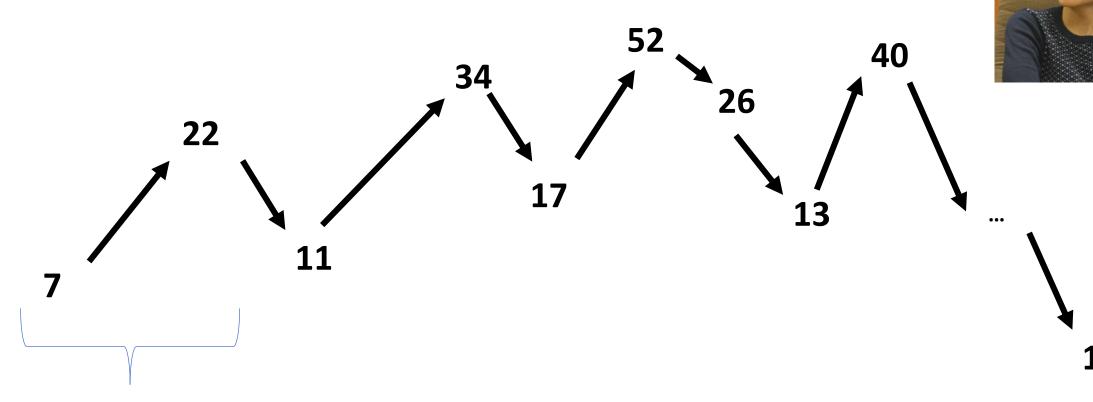






SFI-CSSS, 6th July 2023 page 13 of 17

Walking the walk..

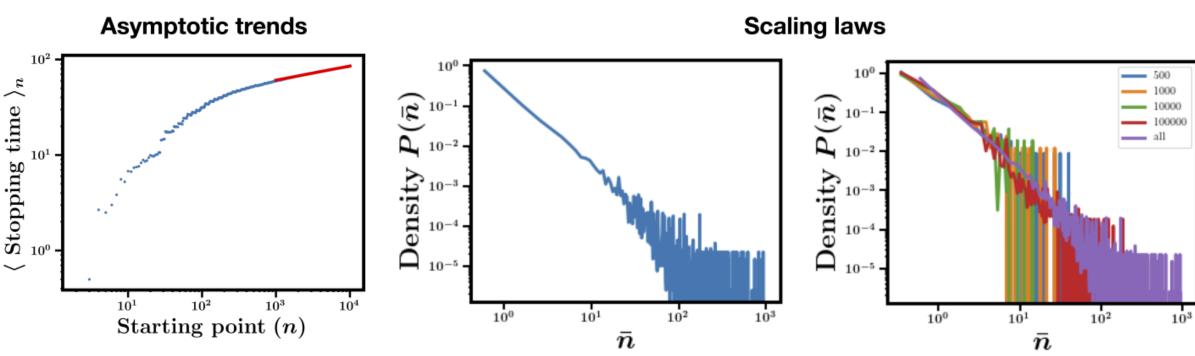


Can we say sth. from the first 2 steps?

SFI-CSSS, 6th July 2023 page 14 of 17

Statistical patterns





SFI-CSSS, 6th July 2023 page 15 of 17

Cris Moore's feedback



Start doing some actual mathematics!

Transform conjecture to p-adic numbers!

Calculate in Nimber number systems and consider it a cellular automaton!

SFI-CSSS, 6th July 2023 page 16 of 17

What's next?

Understand results (neural networks used)

Consensus is to gather the material on Github

Maybe study another problem

SFI-CSSS, 6th July 2023 page 17 of 17