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2



1859: Charles Darwin and «The origin of species»

Natural selection as a central cause of life's diversity

All life originated from a common ancestor

One main area of ignorance:

"The laws governing inheritance are for the most part unknown."



4

6



Solved part of the inheritance problem

Showed that traits can behave like indivisible particles when inherited







1

## 1909: Wilhelm Johannsen

Danish botanist who coined three key concepts

Gene Mendel's particulate units of inheritance (still completely unclear what genes were)

Genotype in modern language: all of an organism's DNA

Phenotype All other observable traits, including fitness



### 1930-1940s: The modern synthesis

Named after a 1942 book by Julian Huxley

Main characters: R.A. Fisher, Sewall Wright, J.B.S. Haldane

Joined three elements The importance of natural selection Mendel's laws of particulate inheritance Population thinking

Created population genetics

Quantitative and mathematical theory that predicts how selection changes a population

Challenging for many biologists



8

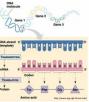
### 1944-: The molecular era

1944: Oswald Avery discovers that DNA is the material basis of inheritance

1953: James Watson and Francis Crick find the chemical structure of DNA

1950s-1960s: transcription, translation, and the genetic code





Wright developed the adaptive landscape to explain essential concepts of population genetics in non-mathematical language



Location: genotype

Elevation: fitness

Wright, Proc. 6th Int. Congr. Genet., 1932

10

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7

Wright developed the adaptive landscape to explain essential concepts of population genetics in non-mathematical language



Evolving population: multiple organisms that explore an adaptive landscape through mechanisms that

1) create variation mutation recombination

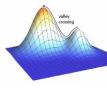
11

 cause differential survival/reproduction natural selection genetic drift

Selection drives evolving populations uphill

Wright, Proc. 6th Int. Congr. Genet., 1932

Wright developed the adaptive landscape to explain essential concepts of population genetics in non-mathematical language

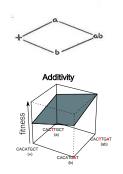


Selection drives evolving populations uphill

On a multi-peaked landscape «things may need to get worse before they can become better»

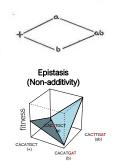
Finding the highest peaks (best-adapted organisms) on a multi-peaked landscape cannot be accomplished by selection alone

### Wright realized that mutations can interact in complicated ways





Wright realized that mutations can interact in complicated ways

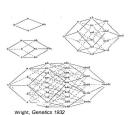




14

### Epistasis can help create multi-peaked landscapes





Wright, Proc. 6th Int. Congr. Genet., 1932

# Adaptive landscapes are vast and multi-dimensional

- A DNA sequence (gene) with 150 base pairs:  $4^{150}{\approx}10^{90}\,\text{possible genotypes}$
- A protein sequence with 150 amino acids:
  - $20^{150} \approx 10^{195}$  possible genotypes (amino acid sequences)

Compare:  $\approx 10^{80}$  hydrogen atoms in the universe

15

13

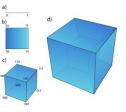
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### Adaptive landscapes are vast and multi-dimensional

Simplified model of genotype: binary string (...0101110101011...)

The 'space' of all possible genotypes becomes a hypercube

Each axis corresponds to one landscape dimension



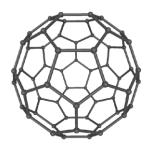
The landscape metaphor can be interpreted in multiple ways

Location	Elevation
genotype	fitness
genotype	any (scalar) phenotype
phenotypic traits (one per dimension)	fitness

Landscape thinking influences many areas of science

Examples:

chemistry operations research psychology Buckminsterfullerenes are complex  $\mathrm{C}_{60}\,\mathrm{carbon}\text{-cages}$  that form in the interstellar medium



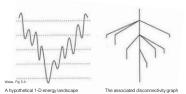
truncated icosahedron 20 hexagons 12 pentagons No pentagons are adjacent



20

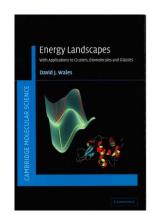
19

Positions of atoms in a molecule can be described by a potential energy landscape

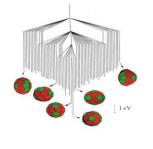


Axes: lengths of chemical bonds Elevation: potential energy (low energy – high stability) Variation generation: thermal energy Minima: stable configurations

21



Buckminsterfullerenes have a complex energy landscape



The disconnectivity graph shows multiple minima near the global minimum

Wales, Fig 8.35.

22

The traveling salesman problem (TSP) is of immense practical and theoretical importance

Task: identify the shortest journey ("tour") that visits each of *n* locations exactly once

Important in operations research energy and time-efficient travel efficient chip design minimizing time to move a telescope through various positions

benchmark problem for combinatorial optimization



A secretary planning a salesman's route with the 'pin and string' method in the 1920s

Cook, Fig. 2.3.

# The traveling salesman problem (TSP) is of immense practical and theoretical importance

A 13,509 US cities tour first solved in 1998



Cook, Fig. 8.8.

26

25



# Many researchers consider human creativity a Darwinian process

The traveling salesman problem (TSP) is of immense

practical and theoretical importance

Location: a journey

Elevation: length of the tour

"a seething caldron of ideas, where ... treadmill routine is unknown, and the unexpected seems the only law...the genius of discovery depends altogether on the number of these **random notions and guesses** which visit the investigator's mind."

> William James, 1880 American philosopher and psychologist

\*I have to compare myself with an Alpine climber, who, not knowing the way, ascends slowly and with toil, and is often compelled to retrace his steps because his progress stopped; sometimes by recarrying, and sometimes by accident, he hits upon traces of a fresh path, which again leads him a little further...\*

> Hermann von Helmholtz, 1891 physician and physicist

28

Pablo Picasso's Guernica

Many researchers consider human creativity a Darwinian process

Psychological Review 1960, Vol. 67, No. 6, 380-400

BLIND VARIATION AND SELECTIVE RETENTION IN CREATIVE THOUGHT AS IN OTHER KNOWLEDGE PROCESSES '

DONALD T. CAMPBELL

## A study on Picasso's process in creating Guernica

Creativity Research Journal 2007, Vol. 19, No. 4, 329-344 Copyright © 2007 by Lawrence Erlbaum Associates, Inc.

The Creative Process in Picasso's *Guernica* Sketches: Monotonic Improvements versus Nonmonotonic Variants Dean Keith Sinonton *University of California, Davis*  A study on Picasso's process in creating Guernica

Picasso drew 45 sketches of Guernica

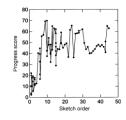
Sketches are temporally ordered from early to late

Simonton shuffled the sketches randomly

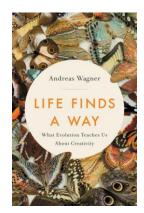
Asked five judges to evaluate their similarity to Guernica

Plotted similarity against temporal order

Picasso's process does not involve simple hill climbing



31



33

A worst-case scenario: Adaptation on a maximally rugged, "uncorrelated" landscape

Biopolymers (DNA, protein) of length N

B possible monomers B=4 for DNA B=20 for proteins B possible genetic variants ("alleles")

B possible genetic variants ("alleles") at each position ("locus") in the string Towards a General Thousy of Adaptive Waika on Rogod Landwayee Struar Kurrawi Desensed Philodoxie ya ad Bepylice, University of Preschanis School of Molocy Handlighte, Prespinatura 1936, UZA Min Store Laws Stores of Enology and Systematic, and Ecosystem Research Center, Central University, Naux, New York 1933, UZA.

J. theor. Biol (1987) 128, 11-45

Example: TACGTCT TACGACT Two alleles at locus 5

B<sup>N</sup> possible genotypes Each genotype has N(B-1) 1-mutant neighbors

34

32

A worst-case scenario: Adaptation on a maximally rugged, "uncorrelated" landscape

### J. sheor. Biol (1987) 128, 11-45

Assign fitness values randomly to each of the  $B^{\rm N}$  possible strings from a some distribution on a real interval (x,y)

Rank all fitness values

Replace fitness values with their rank

Towards a General Theory of Adaptive Walks on Rugged Landscapes

STUART KAUFTMAN<sup>†</sup> artment of Biochemistry and Biophysics, University of Pennsylu School of Medicine, Philadethika, Penerodonaia 1910a, 17 ° 4

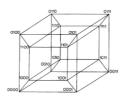
AND Steon Leven tion of Ecology and Systematics, and Ecosystems Research Control

ction of Ecology and Systematics, and Ecosysteme Research Center, Cornell University, Ethaca, New York 14853, U.S.A. A worst-case scenario: Adaptation on a maximally rugged, "uncorrelated" landscape

Simple special case: B=2

2<sup>N</sup> possible genotypes

Assign integers in  $(1, 2^N)$  randomly with uniform distribution to vertices of the hypercube



A worst-case scenario: Adaptation on a maximally rugged, "uncorrelated" landscape

Neighboring genotypes have uncorrelated fitness values

Number of local peaks below the single global peak

$$\frac{B^N}{N(B-1)+1}$$

Scales exponentially in N

37

38

A worst-case scenario: Adaptation on a maximally rugged, "uncorrelated" landscape

Number of peaks that can be reached from the genotype with lowest fitness

 $D^{(log_2D-1)/2} = (N(B-1))^{(log_2N(B-1)-1)/2}$  (upper bound)

Example: N=100, B=20

1.6×10<sup>16</sup> accessible peaks

Total number of peaks 6.7×10<sup>126</sup>

Fraction accessible: 2.4×10-111

2	0
-	ч
-	-

And the state

40

Popular theoretical models of adaptive landscapes

2. Additive model

fitness effect of any one mutation is independent of genotype at other loci single-peaked landscape



Popular theoretical models of adaptive landscapes

A worst-case scenario: Adaptation on a maximally

Popular theoretical models of adaptive landscapes

every mutation can have large effects and thus destroy the "house of cards" of a complex biological system

(upper bound)

rugged, "uncorrelated" landscape

Adaptive random walks step from a genotype to a randomly chosen fitter neighbors with equal probability

Number of steps before such a walk can go no further (has reached a local peak)?

 $log_2 D = log_2 (N(B-1))$ 

Example: N=10, B=20: log<sub>2</sub>D =7.6 N=100, B=20: log<sub>2</sub>D =10.9

1. Uncorrelated model

a.k.a the "house of cards" model

Increases much more slowly than N or B

Reason: number of peaks increases exponentially

3. NK-Model

N loci Fitness contribution of each locus depends on allele at the locus itself alleles at K other loci

Two key parameters: N and K

```
Other parameters:
Distribution of the K loci that influence locus i
(e.g., random and uniform, adjacent, etc.)
Number of monomers B
Distribution of fitness values to assign to each locus and allele
```

Popular theoretical models of adaptive landscapes

# 3. NK-Model

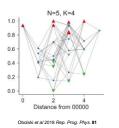
Fitness contribution of locus *i* to genotype g  $w_i(g_i, g_{i_1}, \dots, g_{i_k})$   $B^{K-1}$  possible values of this argument choose as the function values  $B^{K+1}$  random numbers on the interval (0,1) Fitness of genotype g

$$w(g) = 1/N \sum_{i=1}^{N} w_i(g)$$

Popular theoretical models of adaptive landscapes

3. NK-Model

special case K=N-1: uncorrelated model



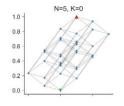
44

43

Popular theoretical models of adaptive landscapes

3. NK-Model

special case K=0: additive model



Obolski et al 2018 Rep. Prog. Phys. 81

45

Popular theoretical models of adaptive landscapes

### 3. NK-Model

0<K<N-1: very complicated landscape structure few analytical results "tunable ruggedness"

46

Popular theoretical models of adaptive landscapes

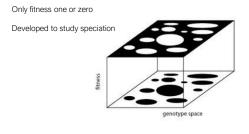
4. Rough Mount Fuji model

$$w(g) = c\eta(g) - d(g, g_p)$$

g<sub>p</sub>...reference (peak) genotype d(g, g<sub>p</sub>)... (Hamming) distance to reference genotype c...constant weight factor n(g)...random variable, uncorrelated among genotypes

c large: uncorrelated c small: single-peaked Popular theoretical models of adaptive landscapes

5. Holey adaptive landscapes



Gavrilets 1997 TREE 12: 307

### Popular theoretical models of adaptive landscapes

6. Models with biophysically/biochemically realistic genotypephenotype relationships



Modelling neutral and selective evolution of protein folding DAVID J. LIPMAN AND W. JOHN WILBUR

Proc. R. Soc. Lond. B (1991) 245, 7–11 From sequences to shapes and back: a case study in RNA secondary structures

PETER SCHUSTER<sup>1,3,3</sup>, WALTER FONTANA<sup>3</sup>, PETER F. STADLER<sup>1,3</sup> AND IVO L. HOFACKER<sup>2</sup>

1/2 - 2 - 2 2/2 - 2 - 2 2/2 - 2 - 2 2 - 2 - 2 2 - 2 - 2 2 -



Evolutionary Plasticity and Innovations in Complex Metabolic Reaction Networks Joio F. Maties Rodrigues<sup>1,24</sup>, Andreas Wagner<sup>1,24</sup> PLoS Computational Biology December 2009 | Volume 5 | Isue 12 | e1000613

Proc. R. Soc. Lond. B (1994) 255, 279-284

49

50

Quantifiers of landscape ruggedness

2. (Semi)local quantifiers

#### Fitness autocorrelation

Along an ensemble of random walks {gt} on the landscape, compute

 $R(t,s) = \frac{M(w(g_t)w(g_{t+s})) - M(w(g_t))M(w(g_{t+s}))}{V(w(g_t))}$ 

(M, V: mean, variance)

Quantifiers of landscape ruggedness

Quantifiers of landscape ruggedness

starting from a given genotype (randomly chosen, low fitness etc.)

determine the fraction of all (shortest) paths to a given peak

1. Global quantifiers

Number of peaks

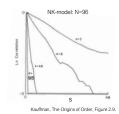
Peak accessibility

(global, high-fitness local etc.)

that are monotonically fitness-increasing

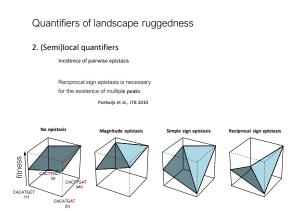
2. (Semi)local quantifiers

Fitness autocorrelation More rapid decay in more rugged landscapes



51

52



Quantifiers of landscape ruggedness

2. (Semi)local quantifiers epistasis of 3<sup>rd</sup>, 4<sup>th</sup> etc. order various approaches Fourier analysis (stader, J. Math. Chem 1996) Walsh transform (Weinreich et al., Curr. Opn. Genet. Dev 2013)

> higher order epistasis may be sparse Affecting few loci/alleles (Poelwijk et al., Nat. Comm. 2019)

# **Empirical landscapes**

## Ammonoid swimming efficiency

Antibiotic resistance evolution TEM-1 beta-lactamase Dihydrofolate reductase

Ribozymes

Gene regulation

55

An adaptive landscape of Ammonoid shell shape

Ammonoids (aka Ammonites) are extinct molluscs Closely related to today's Nautilus

Multichambered spiral shell

Rich fossil record



56

## An adaptive landscape of Ammonoid shell shape

Chamberlain built plexiglass models of Ammonoids with various shell shapes

Dragged them through a water tank

Measured drag coefficient a measure of energy expenditure when swimming



John Chamberlain, Paleontology 1976.

58

57



An adaptive landscape of Ammonoid shell shape

An adaptive landscape of Ammonoid shell shape

Ammonoids had diverse shell shapes Their morphospace can be described

by two parameters W...whorl expansion rate

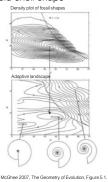
diameter of shell opening relative to distance of coiling axis to inner edge of shell opening

D...distance from coiling axis to inner edge of the shell aperture

The adaptive landscape has two peaks

Fossils cluster preferentially around one peak

Both peaks are occupied discovered later through new fossil finds: Saunders et al., Paleobiology 2004



D McGhee 2007, The Geometry of Evolution, Figure 4.5

# **Empirical landscapes**

Ammonoid swimming efficiency

Antibiotic resistance evolution TEM-1 beta-lactamase Dihydrofolate reductase

Ribozymes

Gene regulation

# TEM-1 beta-lactamase is a model protein for the evolution of antibiotic resistance

Causes resistance against the antibiotic ampicillin

Five DNA mutations suffice to create strong resistance against cefotaxime

Cefotaxime is a WHO «essential medicine»



TEM-1 beta-lactamase is a model protein for the evolution of antibiotic resistance

Weinreich et al., created all 32 combinations of the five point mutations (not all shown here)

5!=120 Shortest paths to the cefotaxime «peak» Fewer than 20% accessible (cefotaxime resistance increasing)

61

62

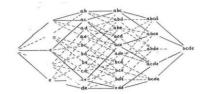
## A renaissance of work on landscapes



Combinatorially complete landscape data is important for landscape analysis

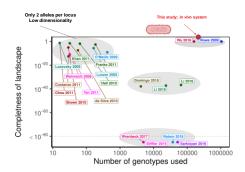
Landscape data is combinatorially complete if the following condition holds for any two genotypes whose phenotype (fitness) has been quantified:

The phenotype (fitness) has also been quantified for all genotypes that lie on each shortest path between the two genotypes



64

63



Andrei Papkou

66

# **Empirical landscapes**

Ammonoid swimming efficiency

Antibiotic resistance evolution TEM-1 beta-lactamase **Dihydrofolate reductase** 

Ribozymes

Gene regulation

### Dihydrofolate reductase (DHFR) is a key enzyme in 1-carbon metabolism

### Mutations at several consecutive amino acids are frequently Involved in the evolution of TMP resistance

15F M201 P21UQ D27E -28R V30R/G/C/ 194L **398P** :153S/V/

CRISPR-Cas genome editing can help to create large libraries of

Observed Frequency

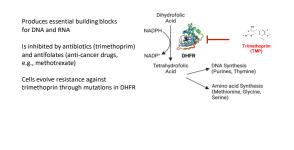
1.0 0.8

0.6

0.4

0.2

0.0



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68

DHFR variants

variants

70

Produce all 4<sup>9</sup>= 262,144 possible variants at 9 consecutive nucleotides encoding A26, D27, L28

Combinatorially complete library

On the E.coli chromosome in vivo

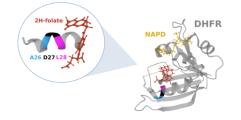
Create a large population of *E.coli* cells in which different cells harbor different

67

A26T/V

Mutations Acquired

Several of these mutations occur at the dihydrofolate binding site



Andrei Papkou

n<sub>x, pre</sub> n<sub>x, post</sub>

10 35 987

39

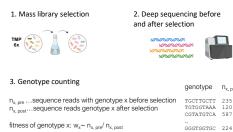
235 120 587

69

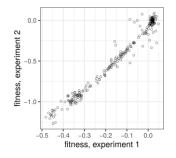
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Mass-selection and deep sequencing can help measure

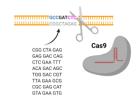
the fitness of all variants in one experiment



Fitness measurements are highly reproducible between experiments



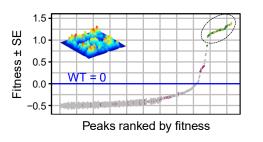
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Tamer, MBE 2019

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The DHFR adaptive landscape harbors 73 fitness peaks far above the wild-type for antibiotic resistance



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73

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74

76

40000

30000

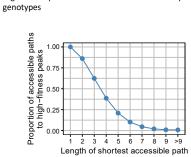
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1 2 3 4 5 6 7 8 9 — peak Genetic distance between peaks (nucleotide sequence)

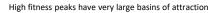
Count

High fitness peaks are accessible even from very distant



75

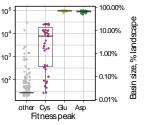




Basin size. # varaints

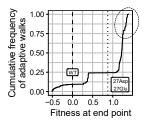


The basins of attraction of each Glu27/Asp27 peak comprise >69% of variants!



Most evolving populations reach a high fitness peak

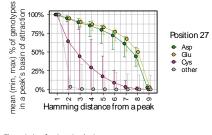
The landscape's peaks are scattered through genotype space



76% of evolving populations reach a high fitness peak Based on 10<sup>6</sup> adaptive walks starting from random genotypes

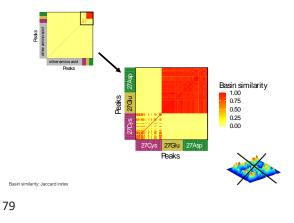
Andrei Papkou

Many genotypes in a peak's basin of attraction are far away from the peak



The majority of variants in a basin also have low fitness (not shown)

The basins of attraction of high peaks overlap greatly

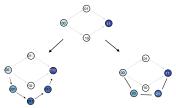


n & Conrad 1994 rilets 1997 TREE Andrei Papkou

Extradimensional by-passes can help overcome fitness valleys

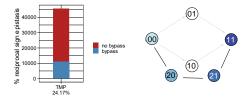
80

Extradimensional by-passes can take various forms



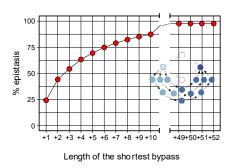
81

25% of fitness dips created by reciprocal sign epistasis can be by-passed with only one extra step.



82

Longer by-passes can help overcome most fitness dips.



Summary

The DHFR antibiotic resistance landscape has many peaks

Despite this ruggedness, high fitness peaks are reached by most evolving populations

Bendixsen et al. PLoS Biology (2019)

# **Empirical landscapes**

Ammonoid swimming efficiency

Antibiotic resistance evolution TEM-1 beta-lactamase Dihydrofolate reductase

Adaptive landscapes of two RNA enzymes

Start from one reference HDV and one reference ligase ribozyme

### Ribozymes

Gene regulation

hey differ at 14 sites

Figure shows only genotypes with fitness >0.07 x reference Node color: dominant activity, node size: activity relative to

Create all 214=16384 possible variants

Measure "fitness" of each variant *in vitro* ability to self-cleave relative to a reference ability to ligate relative to a reference Study landscape with respect to both phenotypes

85

87

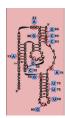
# Adaptive landscapes of two ribozymes (RNA enzymes)

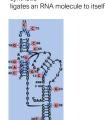
# Hepatitis D virus (HDV) ribozyme

# Class II ligase

synthetic

natural self-cleaving



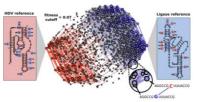


Bendixsen et al. PLoS Biology (2019)

86

### Adaptive landscapes of two RNA enzymes

- The HDV landscape is much more rugged than the ligase landscape 982 peaks vs. 68 peaks
- More than 50% of genotypes (9032) can catalyze both reactions although at very different rates



Bendixsen et al. PLoS Biology (2019

88

### Adaptive landscapes of two RNA enzymes



starting genotypes

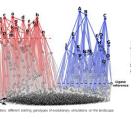
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### Adaptive landscapes of two RNA enzymes

Simulate evolution from a HDV sequence towards a ligase sequence

Assumptions:

- 1. It would be beneficial for an organism to be capable of catalyzing both the cleavage and the ligase reaction
- A gene duplication has created two copies of the gene encoding the selfcleaving HDV enzyme Allows the preservation of selfcleavage ability while 'searching' for genotypes with ligues activity



#### Bendixsen et al. PLoS Biology (2019)

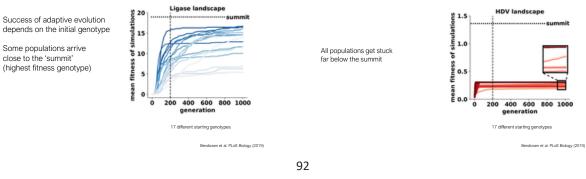
n et al. PLoS Biology (2019

#### Bendixsen et al. PLoS Biology (2019)

### Adaptive landscapes of two RNA enzymes

### Adaptive landscapes of two RNA enzymes

Simulate evolution from a ligase sequence towards a HDV sequence



91

# Summary

Landscape ruggedness varies among RNA molecules

Landscape ruggedness matters for adaptive evolution

Ribozyme promiscuity facilitates adaptive evolution

# **Empirical landscapes**

Ammonoid swimming efficiency

Antibiotic resistance evolution TEM-1 beta-lactamase Dihydrofolate reductase

Ribozymes

### Gene regulation

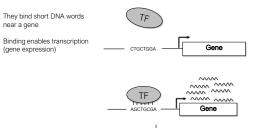
en et al. PLoS Biology (2019)

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93

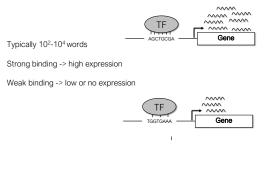


Gene regulation involves proteins called transcription factors (TFs)



### Any one TF can bind multiple DNA words

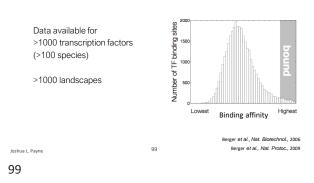
### Large scale measurements allow the analysis of affinity landscapes



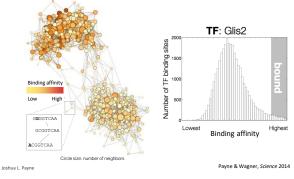
Protein binding microarrays measure the binding strength (affinity) for any Number of TF binding sites one TF to all 48=65536 DNA words of length 8. 50 Only a small subset is bound with high 1000 affinity 50 Construct affinity landscape from these sequences Lowest Highest Binding affinity Berger et al., Nat. Biotechnol., 2006 98 Berger et al., Nat. Protoc., 2009 Joshua L. Payne

97

### Large scale binding affinity measurements allow the analysis of affinity landscapes



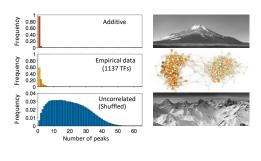
# The affinity landscape of the mouse TF Glis2



100

98

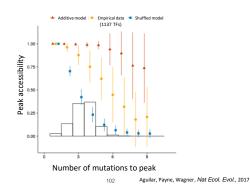
# Landscapes of binding affinity have one to few peaks.



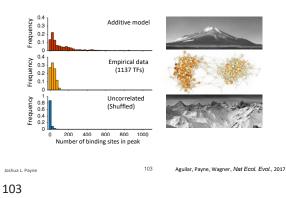
101

Aguilar, Payne, Wagner, Nat Ecol. Evol., 2017

## Peaks are highly accessible via affinity-increasing paths.



Joshua L. Payne



Landscape peaks often comprise many binding sites.

Binding sites from broad peaks should exhibit more genetic diversity than binding sites from narrow peaks.

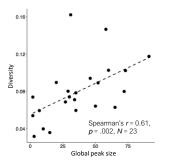
104





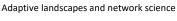
104

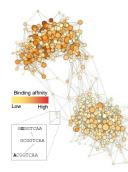
Global peak size correlates with binding site diversity.



Aguilar, Payne, & Wagner, Nat Ecol. Evol., 2017

105

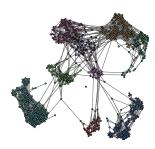




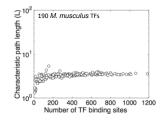
intra-network characteristic path length diameter community structure degree assortativity

106

Adaptive landscapes and network science

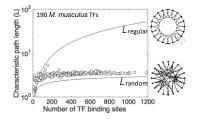


inter-network overlap interface phenotype space covering Genotype networks of TF binding sites are "small-world"



Watts & Strogatz, Nature, 1998 Aguilar-Rodríguez et al., Evolution 2018

## Genotype networks of TF binding sites are "small-world"



Watts & Strogatz, Nature, 1998 Aguilar-Rodríguez et al., Evolution 2018

109

### A successful CSSS project



José Aguilar-Rodríguez Massimo Stella Leto Peel

## The architecture of an empirical genotype-phenotype map

José Aguilar-Rodríguez, Leto Peel, Massimo Stella, Andreas Wagner, and Joshua L. Payne (2018), Evolution 72: 1242–1260.

110

### Summary

Empirical adaptive landscapes of RNA and proteins are somewhat rugged but not prohibitively so

Regulatory landscape are, with some exceptions, smoother

Our knowledge of landscape topography may be highly biased towards landscapes on which adaptive evolution is possible towards regions of a biomolecule that affect fitness strongly

## Outlook

Adaptive «seascapes»

Extradimensional by-passes

Co-evolutionary landscapes

Landscape mapping versus evolution

Landscapes of engineering problems

111

### 112

### Some further reading

Bank, C. (2022) Epistasis and Adaptation on Fitness Landscapes arXiv preprint arXiv:2204.13321, arxiv.org

Szendro, I. G., Schenk, M. F., Franke, J., Krug, J., & De Visser, J. A. G. (2013). Quantitative analyses of empirical fitness landscapes. Journal of Statistical Mechanics: Theory and Experiment, 2013(01), P01005

Obolski, U., Ram, Y., & Hadany, L. (2017). Key issues review: evolution on rugged adaptive landscapes. *Reports on Progress in Physics*, *81*(1), 012602.

Kinney JB, McCandlish DM. (2019) Massively parallel assays and quantitative sequence–function relationships. Annu Rev Genomics Hum Genet. **20**:99–127.